Earthquake-cycle deformation and fault slip rates in northern Tibet

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ABSTRACT

Fault slip rate estimates along the Altyn Tagh and Kunlun strike-slip faults in northern Tibet vary considerably between short-term geodetic and long-term geologic studies. Here we reanalyze and model all global positioning system (GPS) data from northern Tibet to determine if these differences might be explained by previously unmodeled transient processes associated with the earthquake cycle, which can bias slip-rate estimates from geodetic data. We find that these effects cannot reconcile the geodetic data with the lowest **bounds on the geologic slip rates along these faults, even in the presence of low (<1018 Pa s) viscosities within the mid-crust or crust and mantle lithosphere. Surface velocities derived from GPS measurements are best reproduced with models with a high-viscosity (**≥**1018 Pa s) middle to lower crust and mantle lithosphere.**

INTRODUCTION

Fault slip rates inferred from space geodesy sometimes disagree with those determined from geologic studies, which has led some workers to question whether fault slip rates inferred from geodetic surface velocities are representative of those averaged over longer time scales (Mériaux et al., 2004). Nowhere has this discussion been more contentious than in northern Tibet, along the left-lateral Altyn Tagh and Kunlun faults, where slip rate estimates have been used to argue for tectonic models as diverse as eastward rigid-block translation (e.g., Molnar and Tapponnier, 1975) and distributed deformation throughout the lithosphere (Houseman and England, 1986; Royden et al., 1997). Each of these models has support from different data sets: low slip rate estimates of 4–10 mm/yr from geodetic data collected across an ~250 km swath perpendicular to the Altyn Tagh fault (Bendick et al., 2000; Wallace et al., 2004) are cited by some as evidence that deformation is distributed among many faults, while inferences of slip rates of 20–34 mm/yr from geologic data are cited as evidence that since at least 6 ka, eastward translation of rigid Tibetan lithospheric blocks may instead accommodate a large portion of the Indo-Eurasian convergence (Mériaux et al., 2004; Peltzer et al., 1989).

Some workers have sought to attribute the discrepancy in slip rate estimates to systematic errors in geologically determined fault slip rates (e.g., Cowgill, 2007). Alternatively, estimates of fault slip rate from geodetic data may be biased by models that neglect the episodic loading and viscous relaxation of the middle to lower crust and mantle lithosphere that would cause surface deformation rates to vary throughout the earthquake cycle (Hetland and Hager, 2006; Hilley et al., 2005; Johnson and Segall, 2004; Pollitz, 2001; Savage and Prescott, 1978). If transient deformation is neglected in models of geodetic data, inversions could systematically underpredict or overpredict slip rates during different times in the earthquake cycle (e.g., Savage and Prescott, 1978). Previous studies neglected transient deformation processes in models of geodetic data and estimated slip rates by assuming that slip below a locked zone accrues steadily in an elastic half-space over the course of the earthquake cycle. We pose the question, how are surface global positioning system (GPS) velocities, crust and mantle rheology, and long-term fault slip rates within Tibet related through earthquake-cycle effects, and to what extent are previous geodetic

DATA ANALYSIS AND MODELING METHODS

Regional (Shen et al., 2000; Wang et al., 2001; Zhang et al., 2004) and local (Bendick et al., 2000; Wallace et al., 2004) GPS networks constrain the far-field and fault-related motions of northern Tibet, but these networks have never been integrated into a consistent reference frame. We have reprocessed data from regional and near-fault central Asian GPS stations into a common reference frame using the GAMIT/GLOBK software (Herring, 2005; King and Bock, 2005) and applied appropriate corrections to the measurements collected since the 2001 Kokoxili earthquake (see the GSA Data Repository¹). We find that although station velocities that were formerly only referenced to a local network (Bendick et al., 2000; Wallace et al., 2004) have large uncertainties, they are nonetheless consistent with the regional station velocities nearby (Fig. 1). In our model analysis, we describe all station velocities with respect to the stable interior of the Tarim block. We define the rigid-block rotation of Tarim using GPS stations located within its interior, and subtract this motion from the remainder of the geodetic surface velocity field.

These geodetically measured surface velocities (Fig. 1) record the interseismic accrual of strain, while fault slip reflects the release of this strain during frictional failure. Thus, one must model long-term fault slip rates based on limited snapshots of strain accrual rates. Three general classes of models have thus far been employed for this purpose. (1) The interiors of tectonic blocks far from fault boundaries undergo rigid-body rotation (Thatcher, 2007). (2) Rigid-body block rotations are assumed far from fault boundaries, and steady interseismic elastic strain accumulation near faults is modeled with dislocations in an elastic half-space (Savage and Burford, 1973), with the assumption that

estimates of fault slip rates biased by oversimplified models of interseismic deformation? Herein we provide an answer to this question by reanalyzing GPS data from central and northern Tibet and conducting a model exploration of the surface velocity data in the context of time-dependent earthquake-cycle deformation along the Altyn Tagh and Kunlun faults.

¹GSA Data Repository item 2009008, description of GPS processing methods and detailed construction of viscoelastic earthquake cycle block model, as well as supplementary figures, is available online at www.geosociety.org/pubs/ ft2009.htm, or on request from editing@geosociety.org or Documents Secretary, *E-mail: hilley@stanford.edu GSA, P.O. Box 9140, Boulder, CO 80301, USA.

Figure 1. Reprocessed global positioning system surface velocities in northern Tibet including data from Bendick et al. (2000), Wang et al. (2001), and Zhang et al. (2004) (see Data Repository [see footnote 1] for details of analysis). Locations of stars along Altyn Tagh fault and Kunlun fault denote locations at which we present slip rates along these faults in Figure 2. Red ticks along the Altyn Tagh fault and Kunlun fault denote boundaries of rupturing segments defined in earthquake-cycle model. Dashed red lines show **model segment geometries of Altyn Tagh fault and Kunlun fault;** those faults that bound blocks to the east are poorly defined, and so we assume for simplicity that they do not appreciably influence the interseismic strain field. TB, QB, and SB denote locations of rotat**ing spherical caps that represent Tarim block, Qaidam block, and Songpan block, respectively. Blue and green velocity vectors denote best-fi tting model velocities expected late in the earthquake cycle (t/T, time since the most recent earthquake relative to the recurrence interval, = 0.9) for 20-km-thick elastic crust with relaxation time (**τ**) of 200 and 10 yr (corresponding to viscosities of 80 and 4 1018 Pa s), respectively, assuming that earthquakes occur every 300 yr on Altyn Tagh fault and Kunlun fault. Latter scenario approximates low viscosities inferred by Ryder et al. (2007) directly following 1997 Manyi earthquakes. Inferred effective viscosities tended to increase following that earthquake; here we show low-viscosity case to emphasize** effect of low viscosities on the velocity field. Blue and green slip **rates along Altyn Tagh fault and Kunlun fault correspond to each of** the best-fit models described above.

the elastic strain accumulation is completely recovered during earthquakes (Meade, 2007). (3) The current deformation field is assumed to result from distributed viscous flow within the lithosphere (Bendick and Flesch, 2007; England and Molnar, 2005). These models represent various approximations of processes that are likely occurring at different depths in the lithosphere: the upper crust deforms primarily by brittle faulting in which elastic strain accumulation along block boundaries is released during earthquakes, while the middle to lower crust and mantle lithosphere probably flow viscoelastically (e.g., Nur and Mavko, 1974; Savage and Prescott, 1978). In this system, the coupled, time-variable deformation of the elastic upper crust and the flowing lithosphere leaves a potentially large time-dependent imprint on the interseismic surface velocities. When the middle to lower crust and upper mantle readily relax under earthquake-generated stresses, far-field surface velocities may be reduced during much of the earthquake cycle: this may cause the appearance of slow strike-slip deformation rates over broad areas when, in reality, long-term slip rates may be rapid. Deep afterslip or localized shear within the middle to lower crust may also contribute to accelerated surface deformation rates early in the earthquake cycle (e.g., Johnson and Segall, 2004). Time-dependent viscous flow at depth has the potential to reduce velocities at large distances from the zone of strike-slip deformation, which is the requisite condition to accommodate both rapid, longterm strike-slip rates and low interseismic surface velocities.

We assess the impact of earthquake-cycle deformation on surface velocities by modeling elastic strain accrual and release in the upper crust coupled to flow in the underlying Maxwell viscoelastic lithosphere. In the model we treat the upper crust as a series of deforming and rotating blocks in an elastic plate. These blocks are spherical caps that rotate about rotation poles. Small components of convergence or divergence along the block boundaries are accommodated using elastic opening-mode dislocations embedded within the upper elastic plate, such that long-term deformation accrues in the crust surrounding faults as convergence between blocks proceeds. Strike-slip motion between blocks is treated by prescribing a set of vertical faults whose long-term strike-slip rates are determined by the relative motion between rotating blocks. Transient deformation associated with steady interseismic locking and sudden coseismic slip events along the bounding faults is incorporated in the model. For simplicity, we assume that earthquakes occur periodically. At the beginning of each earthquake cycle, an earthquake occurs on a fault in the elastic plate of thickness *H*, with slip magnitude that is equal to the long-term slip rate on the fault multiplied by the earthquake recurrence time (T). These sudden slip events load the viscoelastic lithosphere below, which relaxes stress over a characteristic Maxwell relaxation time (τ) equal to twice the viscosity divided by the shear modulus of the flowing lithosphere (Nur and Mavko, 1974). The flow in the lithosphere coupled to the elastic crust creates a transient postseismic and interseismic phase in surface velocities with duration and magnitude that depends on the ratio of τ/T and the time since the most recent earthquake relative to the recurrence interval (t/T).

We consider three deforming blocks: the Tarim block, bounded on the south by the Altyn Tagh fault, the Qaidam block, bounded on the north and south by the Altyn Tagh fault and Kunlun fault, respectively, and the Songpan block, located south of the Kunlun fault (Fig. 1). Using the measured surface velocities, we determine the best-fitting rotation poles that define the slip rate on bounding faults using a weighted least squares inversion. The reduced chi-square statistic (χ^2_r) , defined as the ratio of the weighted residual sum of squares to the number of degrees of freedom in the model (number of each component of observed velocities minus the number of free model parameters), gauges the misfit between modeled and observed velocities in our analysis. Because the time-dependent component of deformation varies nonlinearly with t/T and τ/T, we compute Greens functions for each component of the rotation poles to perform our least squares inversion for each set of t/T and τ /T considered. By systematically varying t/T and τ /T while inverting for the best-fit rotation pole and computing the χ^2 , we are able to determine how the rheology of the crust and mantle affect the rotation poles, and hence the estimated long-term slip rates along the Altyn Tagh fault and Kunlun fault. Our simple two-layer model additionally assumes that earthquakes along all faults are synchronous and load an infinitely deep viscoelastic material. This provides an end-member scenario in which reduction of far-field velocities due to earthquake-cycle effects are most pronounced.

RESULTS

We varied H , τ/T , and t/T , and inverted for the rotation poles to determine how the layering and rheology of Tibet may affect surface velocities (Fig. 2). Low values of τ/T (corresponding to viscosities $\langle \sim 10^{17}$ Pa s for recurrence times of between 300 and 1000 yr; e.g., Washburn et al., 2001) cause viscous relaxation of the middle to lower crust and mantle lithosphere (referred to hereafter as plastosphere, after Scholz, 1988) to broadly distribute and reduce surface velocities relative to their long-term average throughout much of the earthquake cycle (t/T) in areas south of the Kunlun fault (Fig. 2). Depending on the time in the

Figure 2. Best-fi t slip rates for three-dimensional, two-layer model. A: Altyn Tagh fault (ATF). B: Kunlun fault (KF). Viscosity ranges shown on top of each panel were computed by assuming recurrence times along these faults between 300 and 1000 yr. C: Reduced chi-square misfit statistic for predicted and observed geodetic data. Solid lines in each panel show the case for which $H = 10$ km; dashed lines show **H = 20 km. Letters in A are referenced to model velocities and residuals shown in Figure DR1 (see footnote 1).**

earthquake cycle and the viscosity of the flowing layer (encapsulated by τ/T), flow of the plastosphere may allow model slip rates along the Altyn Tagh fault to reach 12 mm/yr while still matching observed surface velocities. This behavior is generally enhanced by a thicker, elastic crust (larger H) that ruptures during earthquakes (Fig. 2), which loads deeper portions of the flowing plastosphere and forces them to flow more rapidly during the earthquake cycle. As a result, if viscosities of the plastosphere are low, depending on the time in the earthquake cycle, the long-term slip rate along the central Altyn Tagh fault would be systematically underestimated by as much 5 mm/yr in standard slip-rate analyses of the geodetic data (Fig. 2) (e.g., Bendick et al., 2000; Meade, 2007; Savage and Burford, 1973; Wallace et al., 2004).

Should viscosities underneath Tibet be low, our model indicates that slip rates along the Kunlun fault could be as high as \sim 30 mm/yr, if surface velocities are measured late in the earthquake cycle. Along the Altyn Tagh fault, inferred slip rates approach the lower end of estimates derived from block models as the lower layer's viscosity increases (Fig. 2A). Summed slip rates across the Altyn Tagh fault and Kunlun fault generally increase with decreasing τ/T ; however, this increase is accommodated primarily along the Kunlun fault. Nonetheless, in all of the scenarios considered, slip rates along the Altyn Tagh fault are within the broad bounds of 2–12 mm/yr based on our analysis. These geodetically derived slip rates are inconsistent with geologic estimates of 20–34 mm/yr. Geologic estimates of slip rates along the Kunlun fault (9–16 mm/yr; Kidd and Molnar, 1988; Van der Woerd et al., 2002) are much lower than the maximum values permitted by our model. Thus, earthquake-cycle effects cannot reconcile the discrepancy reported between estimates of fault slip rate along these two faults.

The surface velocity field produced by selected models (denoted in Fig. 2) shows how predicted surface velocities compare to those measured for different t/T , τ/T , and H (Fig. DR1). Best-fitting models are those with high viscosities (Fig. 2C), as lower-viscosity scenarios systematically underpredict surface velocities within the Songpan block (Fig. DR1). Also, geologically estimated fault slip rates along the Kunlun fault (9–16 mm/yr) are more consistent with those predicted by high-viscosity scenarios (Fig. 2B). As the thickness of the elastic upper crust increases, observed surface velocities are matched best by high τ/T scenarios (Fig. 2). When all other factors are held constant, increasing t/T requires larger τ/T in the middle to lower crust and upper mantle, while maintaining similar χ^2 values (Fig. DR1). Thus, the observed surface velocities generally tend to favor higher values of τ/T and t/T.

DISCUSSION

These models provide first-order insight into how time-dependent earthquake-cycle deformation involving viscoelastic flow in the interior of the Tibetan Plateau affects the surface deformation and geodetically determined fault slip rates in northern Tibet. We acknowledge that we have made a number of assumptions in our analysis that require further explanation. First, our viscoelastic earthquake-cycle model idealizes the flowing portion of the lithosphere as a Maxwell linear elastic material that is homogeneous, isotropic, and extends to infinite depth. More complicated rheologies have been treated in the context of two-dimensional models (e.g., Hetland and Hager, 2005), and heterogeneities in viscosity within and across lateral, lithospheric-scale boundaries may further affect surface velocities. More complicated models that consider a layered rheology predict that when upper mantle viscosities are low relative to lower crustal viscosities, interseismic velocity gradients near the faults may be pronounced, whereas far-field velocities may be only a fraction of the total transform motion across the boundary late in the earthquake cycle (Johnson et al., 2007, their Fig. 5). This layering could conceivably reconcile high strain rates near the fault with lower far-field velocities that result from the relaxation of the upper mantle. However, layered rheological models of Tibet generally invoke low viscosities in the middle to lower crust relative to the upper mantle (e.g., Klemperer, 2006; Royden et al., 1997). Such a layered viscosity structure produces far-field velocities that are less than would be expected when upper mantle viscosity is used with our simple two-layer model (Johnson et al., 2007, their Fig. 5). A similar reduction in far-field velocities would be expected if a vertical low-viscosity zone extended to great depth beneath the faults; however, these low viscosities would need to persist throughout the middle to lower crust and upper mantle to produce similar effects to a laterally extensive low-viscosity zone.

Our choice of a simple rheology was for expediency and consistency with other earthquake-cycle models (e.g., Pollitz, 2001) and geodynamic models of Tibet. Generally, such simple models are also found to capture much of the observed time-dependent deformation following large recent earthquakes (Bürgmann and Dresen, 2008). With this simple rheology, we are able to treat three-dimensional effects of the northern Tibetan faults in a computationally efficient manner. Our three-dimensional approach captures the first-order relationships between the observed surface velocity field, the fault slip rates that separate rotating blocks, and the flow of the lower portion of the lithosphere during the earthquake cycle.

Our analysis of the GPS data in northern Tibet indicates that earthquake-cycle effects cannot reconcile the reported lower bound on long-term geologic slip rates along the central Altyn Tagh fault with geodetically observed surface velocities. Our models cannot reconcile these data even if plastosphere viscosities are low $\left($ <10¹⁸ Pa s) when earthquake-cycle effects should be most pronounced. Effective viscosities of $4-10 \times 10^{18}$ Pa s (rheological scenario shown in Fig. 1 resulting in 5.6 mm/yr and 25.6 mm/yr of slip along the Altyn Tagh fault and Kunlun fault, respectively) were estimated from the observed postseismic deformation transients of the M 7.6 1997 Manyi earthquake near the western end of the Kunlun fault (Ryder et al., 2007), and suggest that the existence of a thin, low-viscosity layer is not required by the geodetic data. In general, misfits between model predictions and observed surface velocities decrease as the viscosity of the flowing lithosphere increases. In addition, cases in which viscosities are low produce slip rates along the Kunlun fault well in excess of those inferred based on surface offsets along its central portion (9–16 mm/yr; Kidd and Molnar, 1988; Van der Woerd et al., 2002). Thus, our models indicate that the observed surface velocity field is most consistent with a scenario in which relatively slow slip rates characterize the boundaries of elastic, rotating blocks, under which a relatively high-viscosity middle to lower crust and mantle are present (Bendick et al., 2000; Meade, 2007; Wallace et al., 2004).

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Data Repository Material

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Model Construction

Our model is a three-dimensional viscoelastic earthquake cycle model consisting of faults in an elastic lithosphere overlying a Maxwell viscoelastic asthenosphere (Johnson and Fukuda, manuscript in preparation). The model incorporates both long-term and interseismic crustal motions using the back-slip model concept that originated with Savage and Burford [1973] and Savage [1983]. The principal idea of these back-slip models is that the interseismic velocity field can be decomposed into: 1. a steady, long-term velocity field in which faults slide at the long-term slip rate, and 2. a transient perturbation to this steady-state due to locking of faults during the interseismic period. Interseismic locking of faults is modeled with backwards slip to cancel the long-term velocity discontinuity. The solution for a dislocation in an elastic half-space Savage and Burford [1973]) or in an elastic plate overlying a viscoelastic substrate Savage and Prescott [1978]) was adopted for the back-slip part of the solution. The back-slip models assume no steady-state strain in the fault bounded blocks. The 3D elastic half-space versions of this model (e.g., McCaffrey [2002], Meade and Hager [2005]) are directly analogous to the 2D elastic model of Savage and Burford [1973]. In the 3D models, fault-bounded blocks rotate undeformed over the long term about Euler poles and interseismic elastic strain is introduced with backwards slip on dislocations in an elastic half space.

We developed the solution for a dislocation in an elastic plate overlying a Maxwell viscoelastic substrate using the method of propagator matrices and the correspondence principal for viscoelasticity. The formulation is essentially identical that of to Fukahata and Matsu'ura [2006] and we refer the reviewer to this work for a mathematical formulation of the solution.

The viscoelastic block model used in this paper is analogous to the 2D Savage models for faults in an elastic layer overlying a viscoelastic half-space (Savage and Burford [1973]), Savage and Prescott [1978]). We model the interseismic deformation field as a superposition of a steady-state, long-term velocity field (with no fault locking) and an interseismic perturbation to this steady state due to periodic locking and unlocking of faults in an elastic lithospheric plate overlying a Maxwell viscoelastic asthenosphere.

Long-term, steady-state velocity field

We adopt a kinematic steady-state velocity field as an extension of elastic half-space block models developed by McCaffrey [2002] and Meade and Hager [2005]. In the elastic half-space block models, the steady-state velocity field is defined by rigid-body rotations of blocks about Euler poles which result in faultnormal and fault-parallel velocity discontinuities across faults and purely horizontal block motions. Our method is based on this idea, but we modify the block motion to remove fault-normal velocity discontinuities. Our steady-state velocity field satisfies the following slip conditions on faults: 1. the fault-normal component of velocity discontinuities across faults is zero, 2. the strike component of slip rate on faults is equal to the strike component of velocity discontinuity across faults resulting from rigid block motions. The first condition guarantees that fault surfaces do not open or inter-penetrate.

The steady-state surface velocity field is obtained by summing three separate velocity fields. We begin with rotations of blocks bounded by faults defined by Euler poles of rotation. The fault-normal components of velocity discontinuities across faults are canceled by adding the velocity field generated by steady opening or closing of the faults. The cancellation of fault normal discontinuities is computed using the solution for a dislocation with steady tensile slip in an elastic plate overlying a viscoelastic half space.

Perturbation to steady state: Earthquake cycle

Our formulation of the earthquake cycle is nearly identical to the formulation presented Matsu'ura and Sato [1989]. Areas of faults that are locked during the interseismic period are modeled with steady back-slip to cancel the long-term velocity discontinuity across the fault. Periodic earthquakes on the locked section are modeled with an infinite sequence of periodic slip events on the locked sections. Steady backslip is modeled with steady creep on a fault in an elastic plate. Periodic earthquakes are modeled by imposing an infinite sequence of sudden slip events on the faults such that the coseismic slip divided by the earthquake recurrence time is equal to the long-term fault slip rate. As shown by Matsu'ura and Sato [1989], the sum of an infinite number of solutions for a single earthquake imposed at a regular recurrence interval can be obtained analytically.

Formulation of model for Tibet

We cast surface velocities in terms of two Rotation Poles (RPs) representing rotation of the Qaidam and Songpan blocks relative to stable Tarim, and the earthquake cycle parameters, t/T and t/T. We then select fixed values for t/T and t/T, and invert the GPS velocity field for the RPs, from which slip rates along the KF and ATF are derived (described below).

We calculate velocities due to rigid-block rotations directly from the RPs, the angular location of each of the geodetic station, and the radius of the earth as described in McCaffrey [2002] and Meade and Hager (2005). This defines how rigid-body rotations within the spherical caps change with changing rotation poles. To ensure that the surface velocity distribution remains continuous at the surface, we discretize the boundaries of each of the rotating spherical caps into planar segments. During the interseismic period we impose back-slip on each segment at a rate that exactly opposes the rotation accommodated between blocks. This is

accomplished by resolving the velocity due to the rotation described by the RPs onto each side of each of the planar segments to determine the relative displacement rate across each of these segments. This back-slip is imposed on a dislocation extending over the entire thickness of the elastic layer for both strikeslip and opening-mode components of the velocities. Finally, we assume that earthquake-cycle deformation occurs as the result of discrete strike-slip earthquake events along the block boundaries. At the beginning of the earthquake cycle, a uniform displacement equal to the strike-slip rate along each of the defined fault segments times the recurrence interval is imposed over the planar dislocation that extends the entire depth of the upper, elastic layer.

For simplicity, in this study, all earthquakes along all segments are synchronous and share a common recurrence interval, which does not change over time. We explored the effect that asynchronous earthquakes would have on surface velocities, which we describe below.

Surface velocities vary linearly with the components of the RPs for both the rotation and backslip components of our model, allowing us to perform a standard linear least-squares inversion of the geodetic data to determine the RPs for these components for fixed values of t/T and t /T. However, the time-dependent surface velocities are nonlinearly related to t/T and t /T. To exploit a linear inversion for this problem, we progressively fix values for t/T and t/T to specify the timedependent, non-linear component of the modeled surface velocities and scale this contribution with the strike-slip rate that results from each component of each RP on each fault segment. This contribution is summed with that due to rigid-block rotation and backslip, and a linear inversion is performed. The best-fit RPs was used to determine the reduced chi-square statistic for the model fit to the data. Next, the values of t/T and t/T were varied, and each set of best-fit RPs was used to calculate each reduced chi-squared value as a function of t/T and t /T. From each of the best-fit RPs, the slip rates along the ATF and KF were determined by resolving the surface velocities due to the rotations onto the fault segments.

In our model, we specified all earthquakes along fault segments to be synchronous. In addition, we considered only a single lower viscoelastic layer of infinite extent in our modeling. Both of these factors are clearly oversimplifications. We explored the first of these effects by systematically varying the value of t/T for each segment. We found that when t /T was large, a spatially varying t/T did not appreciably impact the velocity field. However, as t /T was decreased, surface velocities along different segments became quite variable depending on the relative time in the earthquake cycle. This caused modeled surface velocities to vary significantly in space, depending on the time since the last earthquake along each of the segments. In contrast, the observed surface velocities are continuous in space and do not show the significant excursions expected when lower layer viscosities are low and t/T varied appreciably between fault segments. Thus, either t/T is small and t/T is the same, or t /T is large when viewed in the context of our simple two-layer model. This

lends further support to the hypothesis that t /T is likely large in the area, or else it is very coincidental that we do not see such pronounced variations in space that might be expected if t /T was small and t/T was variable for each of the segments. In the end, we chose not to include the results of this modeling in the text, because of the lack of high-quality paleoseismic data along these faults that would be required to perform a meaningful calibration of the model in which t/T was allowed to vary according to each segment.

The second assumption of our model is that the lower viscoelastic layer extends to an infinite depth. In Tibet, a layered viscosity structure may be appropriate based on some geodynamic models of the area (e.g., Royden et al., 1996). Based on our previous work in the Mojave, such layering could mask the presence of a low viscosity zone in the lower crust of Tibet. However, such masking does not affect our conclusion that viscoelastic earthquake cycle effects cannot be invoked to reconcile high geologically determined slip rates with low geodetically measured surface velocities in the region.

Lateral contrast in lithosphere thickness

It has been proposed that the any low viscosity channel under Tibet does not extend into the Tarim basin to the north of the ATF. Therefore our simplified 3D block model with a uniform elastic thickness and uniform schizosphere viscosity may not be completely analogous to the conditions of the lithosphere surrounding the ATF. Here we utilize a boundary element model to examine the influence of a change in elastic lithosphere thickness across the fault on the surface velocity pattern.

As illustrated in Figure DR2, we model an infinitely long strong strike-slip fault in elastic lithosphere overlying a Maxwell viscoelastic asthenosphere. As in the 3D models, the fault is locked during the interseismic period and sudden periodic slip is imposed on the fault to represent earthquakes. We model a 2000 km-wide shear zone in which we impose half the long-term fault slip rate at both ends of the elastic lithosphere such that the fault slips to keep up with the relative motion of the edges of the shear zone. The upper ground surface is traction-free. For simplicity, the edges of the asthenosphere are also assumed to be traction free, however the results are generally not sensitive to the choice of boundary conditions for the edges of the asthenosphere.

Figure S3 illustrates velocity profiles generated with the variable-thickness boundary element model assuming the geometry shown in Figure DR2. Profiles are shown for two different ratios of recurrence time of earthquakes, T, to relaxation time of asthenosphere, t and for different times, t, since the last earthquake. For comparison, the Savage and Prescott [1978] model with an elastic plate of uniform thickness of 15 km is shown for the same earthquake timing parameters. Surface velocities scale linearly with fault slip rate, so normalized surface velocities are plotted. The lithospheric thickness change across the faults introduces an asymmetry in surface velocities that are more pronounced for

smaller t/T ratios (lower viscosity asthenosphere or longer recurrence times). Strain rates are generally lower on the side of the fault with the thicker lithosphere. The surface velocities at a distance of 500 km from the fault are similar for the uniform thickness and variable thickness models, however the shape of the velocity profiles are different.

As an idealized analog for the ATF bounded by the thick crust of the Tarim Basin and the perhaps thinner crust of the Tibetan Plateau, we use the model geometry illustrated in Figure DR2. We assume the last large earthquake on the ATF occurred 600 years ago with an earthquake recurrence time of 1000 years (e.g., Washburn et al., 2001). Figure S3 shows fault-parallel GPS velocities at sites near the center of the ATF projected onto a profile perpendicular to the fault as well as model velocity profiles for different asthenosphere viscosities. The error bars on the data are 1s. For each asthenosphere viscosity shown in Figure S3, we have adjusted the fault slip rate by eye to best match the observed velocity profile in a qualitative sense. The curves are labeled with this slip rate.

The data are not of sufficiently high quality to determine the degree of asymmetry in velocity profile across the ATF. The model curves show that the data are reasonably well reproduced with the variable-thickness model for asthenosphere relaxation times of 2×10^{19} Pa s or higher and slip rates of 10-12.5 mm/yr. The model with asthenosphere viscosity of 10^{19} Pa s displays a degree of asymmetry in velocity profile that is perhaps not seen in the data, but is right at the edge of what can be inferred given the low signal to noise ratio of the data.

To examine the extent to which neglecting lateral variations in lithosphere thickness in our 3D models might bias estimates of fault slip rate, we conduct synthetic inversions. We generate two synthetic data sets using the boundary element model surface velocity profiles for asthenosphere viscosities of 2×10^{19} Pa s and 10^{20} Pa s, recurrence time of 1000 years, time since last earthquake of 600 years, and slip rate of 15 mm/yr. The lithosphere geometry is as shown in Figure DR2. We add Guassian noise to the data and invert for fault slip rate, elastic thickness and recurrence time using the Savage and Prescott [1978] model assuming the time since the last earthquake is known. The Savage and Prescott [1978] model is analogous to our 3D earthquake cycle model, so this serves as a logical test of the model assumptions in our model for Tibet. The synthetic data sets are shown in Figure S5. We estimate posterior probability distribution for parameters using a Monte Carlo-Metropolis sampling algorithm and the marginal posterior distributions for parameters are shown as histograms in Figure S5. The 'true' values are shown with green bars. The important result is that the estimate fault slip rates are only slightly lower than the true slip rates (within 90% of the true values). Therefore we conclude that the fault slip rate inferences from the 3D earthquake cycle model that we use in this paper are not significantly biased by our assumption of uniform elastic thickness.

Data Processing

We reprocessed data from 21 GPS station locations reported in Bendick et al. (2000) and Wallace et al. (2005) to integrate these velocities into the ITRF2000 reference frame. These data were processed together with Asia fiducial sites (IGS for 1994 and 1998; IGS+CMONOC for 2002) using GAMIT, using loosely constrained daily solutions are output for site positions, orbits, and pmu parameters. Reprocessed GPS sites are listed in Table 1, while fiducial sites are listed in Table 2. The above solutions were combined with SOPAC loosely constrained daily global solutions using GLOBK, and combined loosely constrained daily solutions were output with orbital parameters surpassed.

During the observation period, the 2001 Kokoxili earthquake resulted in coseismic ground deformation that required adjustments of the observed surface positions. To do this, coseismic displacements for the 2001 Kokoxili earthquake were calculated at sites using a fault slip model obtained through inversion of GPS and observed surface slip data. The daily SINEX files were modeled to estimate site positions, velocities, and coseismic deformation using QOCA. A group of IGS sites were constrained to their ITRF2000 velocities with uncertainties of 2, 2, and 5 mm/yr for the east, north, and up components respectively. The coseismic deformation due to the 2001 earthquake was constrained by the prior estimates of the modeled surface deformation field using the following uncertainties: $(0.6D_i)^2 + (0.3D_j)^2 + (0.3D_k)^2$, where D_i , D_j , and D_k are the uncertainties in the coseismic displacements in the x, y, and z directions, respectively.

Once the ITRF2000-referenced surface velocity field was computed (presented in Table 3), we used a set of sites within the interior of the Tarim Basin (listed in Table 4) to determine the best-fitting rotation pole of this block. All station velocities were adjusted to this rotation pole to form a Tarim-Basin-based reference system, within which the modeling was carried out. GPS velocities referenced to this rotation pole are reported in Table 5.

SOM Table DR1: Reprocessed Site Names from Bendick et al. (2000) and Wallace et al. (2005)

SOM Table DR2: Feducial Site Names

SOM Table DR4: Sites Used to Define Tarim Reference (Reported Locations in Zhang et al., 2005)

SOM Table DR5: Sites in Tarim-Block-Based Reference Frame Used in Modeling

Figure DR1: Observed and modeled surface velocities (A-C) and vector difference between observed and modeled velocities (residuals; D-F) for scenarios shown in Figure 2. The first column highlights the impact of changing t/T , the second t/T (B, E) and the third $H(C, F)$.

Figure DR2. Illustration of boundary element model designed to examine the influence of variable elastic thickness on surface velocity pattern. The model is antiplane strain (all motions in and out of paper). Red fault is infinitely long strike-slip fault with imposed periodic earthquakes. Fault is locked between earthquakes. A 2000 km-wide shear zone is driven at constant far-field relative velocity of 15 mm/yr.

Figure DR3. Surface velocity profiles generated with boundary element model shown in Figure DR2 (blue curves). Profiles are shown for two different ratios of recurrence time, T, to relaxation time, t, and at different times since the last earthquake, t. For comparison, surface velocities predicted by the Savage and Prescott [1978] model are shown in red for the same earthquake times, relaxation times, and elastic plate thickness of 15 km. Surface velocities are normalized by fault slip rate. The asymmetry in the velocity profiles introduced by abutting plates of different thickness is more pronounced for the lower viscosity case (a).

Figure DR4. Profile of GPS velocities across central part of ATF. Error bars are 1s uncertainties. Curves are surface velocity profiles generated with the variable lithosphere thickness model in Figure DR2. The curves are generated assuming a periodic earthquake recurrence interval of 600 years and 300 years since the last earthquake. Slip rate is adjusted "by eye" to qualitatively fit the GPS data. Lithosphere geometry is shown in Figure DR1 and curves are labeled with asthenosphere viscosities and slip rates.

Figure DR5. Synthetic inversion results. Guassian noise was added to profiles shown in Figure S3 and synthetic data were inverted for parameters assuming the Savage and Prescott [1978] earthquake cycle model. Time since last earthquake is assumed known and other parameters are estimated using a Monte Carlo-Metropolis inversion. Histogram plots represent posterior probability distributions of parameters. Synthetic data with 2s uncertainties and shown in bottom right panels. Red curves are posterior 2s model predictions.