

# Determination of Local Magnitude Using BDSN Broadband Records

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**Abstract** The Berkeley Seismographic Station operated standard Wood–Anderson torsion seismographs from 8 April 1928 through 16 January 1994. These seismographs are historically significant in that their seismograms have been used to determine local (Richter) magnitude of earthquakes that occurred in northern and central California and adjacent regions, routinely since 1948 and *ad hoc* back to 1928. Broadband digitally recording seismographs were co-sited at four stations with Wood–Anderson instruments to compare the records. The Wood–Anderson seismographs became redundant for the purpose of determining the maximum horizontal trace amplitudes once procedures were developed to synthesize their seismograms accurately from the broadband digital recordings. Operation of the Wood–Anderson seismographs was subsequently discontinued. This article demonstrates the ability to determine an unbiased measure of local magnitude from synthesized Wood–Anderson seismograms, thereby maintaining a seamless catalog of local magnitude at Berkeley.

## Introduction

The local magnitude (hereafter denoted  $M_L$ ) for earthquakes, occurring in northern and central California and adjacent regions, has been routinely determined by Berkeley and reported in the *Bulletin of the Seismographic Stations of the University of California* since 1948 (Romney and Meeker, 1949). The main use of the  $M_L$  scale has been to provide a simple and quantitative measure of the relative size of earthquakes.  $M_L$  is determined from the “maximum trace amplitude” recorded photographically by “standard 0.8-sec-period Wood–Anderson torsion seismographs” (hereafter denoted WA) (Richter, 1935; Gutenberg and Richter, 1942; Richter, 1958).

As shown by Uhrhammer and Collins (1990), synthesized Wood–Anderson (hereafter denoted SWA) seismograms can be routinely generated from horizontal-component broadband digital records (with sampling rates of 20 samples/sec or higher), for the purpose of determining the maximum trace amplitude. When generating SWA records, it is crucial to note that the response of WA seismographs of the type operated in the UC Berkeley station network is  $V_S = 2080$ ,  $T_S = 0.8$  sec, and  $h_S = 0.7$  critical (Uhrhammer and Collins, 1990) and not  $V_S = 2800$ ,  $T_S = 0.8$  sec, and  $h_S = 0.8$  as has been commonly assumed and reported repeatedly in the seismological literature since the original article of Anderson and Wood (1925).

The goal of this study is to verify the successful generation of SWA seismograms through comparison of maximum amplitudes and waveforms and subsequently determine station magnitude adjustments (hereafter denoted  $\delta M_L$ ) for the determination of  $M_L$  using the recently upgraded

broadband instrumentation in the Berkeley Digital Seismic Network (BDSN) in northern and central California (Romanowicz *et al.*, 1992). The overall aim is to be able to continue the reporting of  $M_L$ , as has been done routinely since 1949 and *ad hoc* for events of interest dating back to 1927, without introducing a significant bias into the Berkeley earthquake catalog.

## Historical Perspective

WA seismographs operated continuously longer than any other instrument to date in the Berkeley seismographic network. WA seismographs began operating at Lick Observatory on top of Mt. Hamilton (MHC) on 8 April 1928 (Uhrhammer, 1989), and they operated continuously until 16 January 1993. Dates of operation of the five Berkeley stations housing WA seismographs and of the BDSN broadband stations used in this study are presented in Table 1.

WA seismographs became particularly important after Richter (1935) introduced the concept of an instrumental earthquake magnitude scale in which the “local magnitude ( $M_L$ )” is determined from

$$M_L = \log A - \log A_0(\Delta) + \delta M_L, \quad (1)$$

where  $A$  is the maximum trace amplitude recorded on a WA seismogram,  $A_0(\Delta)$  is a distance ( $\Delta$ )-dependent attenuation function, and  $\delta M_L$  is a station-dependent  $M_L$  adjustment. A detailed history and development of the  $M_L$  scale is presented by Boore (1989). Routine reporting of  $M_L$  in the *Bul-*

Table 1  
BDSN Station Information

Stn	Lat	Lon	Elev (m)	Inst	Dates* of Operation	Site	Lithology†	$\mu$ ‡	$\kappa$ §
ARC	40.877	-124.075	60.0	WA STS-2	06/20/52-01/15/93 05/28/92-current	Ground floor	Sandstone	1.4 1.1¶ (2.6)	-0.2
BKS	37.877	-122.235	276.0	WA STS-1	07/01/62-01/16/93 05/11/87-current	Mining drift	Shale	(2.6)	-1.3
BRK	37.873	-122.260	81.0	WA STS-2	01/01/34-05/31/62 02/01/94-current	Basement pier	Franciscan	27	0.0
CMB	38.035	-120.385	719.0	STS-1	07/01/86-current	Surface vault	Limestone	3.1	0.0
HOPS	38.994	-123.072	299.1	STS-1	03/01/95-current	Buried vault	Franciscan	2.7	+0.3
JRSC	37.404	-122.238	103.0	STS-2	06/30/94-current	Surface vault	Serpentine	1.2	-0.3
KCC	37.324	-119.318	914.3	STS-1	12/08/95-current	Tunnel	Granite	3.4	0.0
MHC	37.342	-121.642	1282.0	WA STS-1	04/08/28-01/16/93 09/10/86-current	Ground floor	Graywacke	1.4   (3.0)	+1.1
MIN	40.345	-121.605	1495.0	WA STS-1	01/02/39-01/15/94 03/19/93-current	Surface vault	Tuff	0.7	0.0
ORV	39.556	-121.500	360.0	STS-1	07/24/93-current	Surface vault	Basalt	3.5	0.0
PKD1	35.889	-120.425	5.0	STS-2	10/22/91-current	Concrete slab	Quaternary	0.7	-1.2
SAO	36.765	-121.445	350.0	STS-1	01/28/88-current	Buried vault	Granite	2.8	-0.6
STAN	37.404	-122.174	158.0	STS-2	04/01/91-06/30/94	Building slab	Alluvium	0.3	+0.1
WDC	40.580	-122.540	300.0	STS-2	07/14/92-current	Mining drift	Gneiss	4.5	-0.5
YBH	41.732	-122.711	1100.0	STS-1	07/24/93-current	Mining drift	Metavolcanic	4.6	-1.0

\*Dates of operation of WA and digitally recorded BDSN instruments.

†Bedrock lithology.

‡Estimated site rigidity in units of  $10^{11}$  dynes/cm<sup>2</sup>.

§Estimated terrain curvature in km<sup>-1</sup>.

¶ $\mu$  for dominant subsurface Orinda formation underlying BKS (David L. Jones, personal comm. 1995).

|| $\mu$  for dominant subsurface Franciscan sandstones underlying MHC (David L. Jones, personal comm. 1995).

letin of the Seismographic Stations began in 1948 (Romney and Meeker, 1949).  $M_L$  for earthquakes occurring prior to 1948 was estimated on an *ad hoc* basis and tabulated in Bolt and Miller (1975).  $M_L$  was determined to 0.1 resolution back to 1942 and to 0.5 resolution prior to 1942. Only a few events have an assigned  $M_L$  prior to March 1934.

$M_L$  was routinely calculated by using the Nordquist nomograph (Gutenberg and Richter, 1942) prior to the advent of personal computers (PC's) in the Seismographic Station. The historical  $\delta M_L$  shown in Table 2 was used when calculating  $M_L$ . When PC's were installed, in 1984, an algorithm was developed and used for the calculation of  $M_L$ . When the digitally recorded BDSN broadband instrumentation came on-line in 1986 (Bolt *et al.*, 1988), algorithms were developed and used for calculation of  $M_L$  from the maximum trace amplitudes registered on SWA seismograms.

### Methodology

The primary goal is to maintain continuity in the determination of  $M_L$  as the metrology has evolved from analog to digital instrumentation. A related goal is to maintain the simplicity of Richter's original methodology for determining  $M_L$  as given in equation (1) and described in his 1935 article. The analysis consists of four steps designed with the aim of verifying that a seamless continuity in the determination of

Table 2  
BDSN  $\delta M_L$

Station	$\delta M_L$ (Historical)	$\delta M_L$ (this study)
ARC	+0.2*	+0.209 ± 0.028
BRK	+0.2†	+0.198 ± 0.033
BKS	0.0*	-0.035 ± 0.017
MHC	+0.1†	+0.128 ± 0.018
MIN	-0.1*	-0.107 ± 0.026

\*Tocher (personal comm., 1979)

†Gutenberg and Richter (1942).

$M_L$  can be maintained when converting from measuring the maximum trace amplitudes on WA seismograms to measuring them on SWA seismograms. First, we verify the historical  $\delta M_L$  that was used in the routine determination of  $M_L$  from the WA seismograms using events in Fig. 1. Then, we describe how the SWA seismograms are routinely generated for the purpose of measuring the maximum trace amplitudes. Next, we compare WA seismograms with the corresponding SWA seismograms, at the four sites that housed both WA seismographs and broadband seismographs, and determine  $\delta M_L$ 's for use with the SWA seismograms. Finally, we determine  $\delta M_L$ 's for use with the rest of the BDSN broadband stations using events in Fig. 2.

When calculating  $\delta M_L$ 's for the BDSN stations, we dis-

covered that there were systematic variations in the  $M_L$  residual distribution with both distance and azimuth. However, in keeping with the original methodology of Richter (1935), we solve only for perturbations to the attenuation function  $[-\log A_0(\Delta)]$ .

### Verification of the Historical $\delta M_L$ 's

To verify the historical  $\delta M_L$ 's (Table 2) used in the routine determination of  $M_L$  from WA seismograms, we proceed in two steps: first, determine simultaneously the  $\delta M_L$ 's for ARC, BKS, MHC, and MIN; then, solve for the  $\delta M_L$  for BRK by comparison with BKS. In the simultaneous least-squares inversion for the  $\delta M_L$ 's at ARC, BKS, MHC, and MIN, we require that every event used in the inversion be recorded on-scale by all eight WA's (two components at each station) with an amplitude of at least 0.3 mm, and we impose the constraint that the sum of the  $\delta M_L$ 's is stationary. This guarantees that the  $M_L$ 's for each event will be identical, hence unbiased, when using either the historical  $\delta M_L$ 's or the least-squares-derived  $\delta M_L$ 's. The  $\delta M_L$  for BRK is solved for separately by comparison with BKS because WA's have not been operated at BRK since BKS was opened in 1962.

Between 1984 and 1992, 71 earthquakes, listed in Appendix A and plotted in Figure 1, that occurred in central and northern California and vicinity were recorded by the WA's at ARC, BKS, MHC, and MIN and met the above criteria. The stationarity constraint requires that the sum of the least-squares-derived  $\delta M_L$ 's is +0.2, the same as the sum of the historical  $\delta M_L$ 's at the ARC, BKS, MHC, and MIN. The results are given in Table 2. Note that the least-squares-

derived  $\delta M_L$ 's are the same as the historical  $\delta M_L$ 's when rounded to the nearest tenth. Thus we have verified the historical  $\delta M_L$ 's for these four stations.

A BDSN broadband seismograph was installed temporarily at BRK, on the original WA pier in Haviland Hall on the Berkeley campus, in order to record some events for comparison with BKS. The WA at BKS was already discontinued, so we compared the corresponding SWA seismograms at BRK and BKS for five regional earthquakes, and the inferred  $\delta M_L$  for BRK is given in Table 2. Note that the SWA-derived  $\delta M_L$  is not significantly different than the historical  $\delta M_L$ . Thus we have also verified the historical  $\delta M_L$  for BRK.

### Generation of SWA Seismograms

SWA seismograms are routinely generated, for the purpose of measuring the maximum trace amplitudes, using frequency domain convolution. The response of WA seismographs is described in detail by Uhrhammer and Collins (1990), and calibration parameters for the individual WA seismographs in the Berkeley network are given in Appendix B. We adopt the complex pole pair:

$$s(\omega) = V_S \cdot [\omega_S h_S \pm i \omega_S (1 - h_S^2)^{1/2}], \quad (2)$$

where  $V_S = 2080$ ,  $h_S = 0.7$ ,  $\omega_S = 2\pi/T_S$ , and  $T_S = 0.8$  sec as the representative displacement frequency response of a WA seismograph, for use in calculating SWA seismograms. This is essentially equivalent to a two-pole high-pass But-

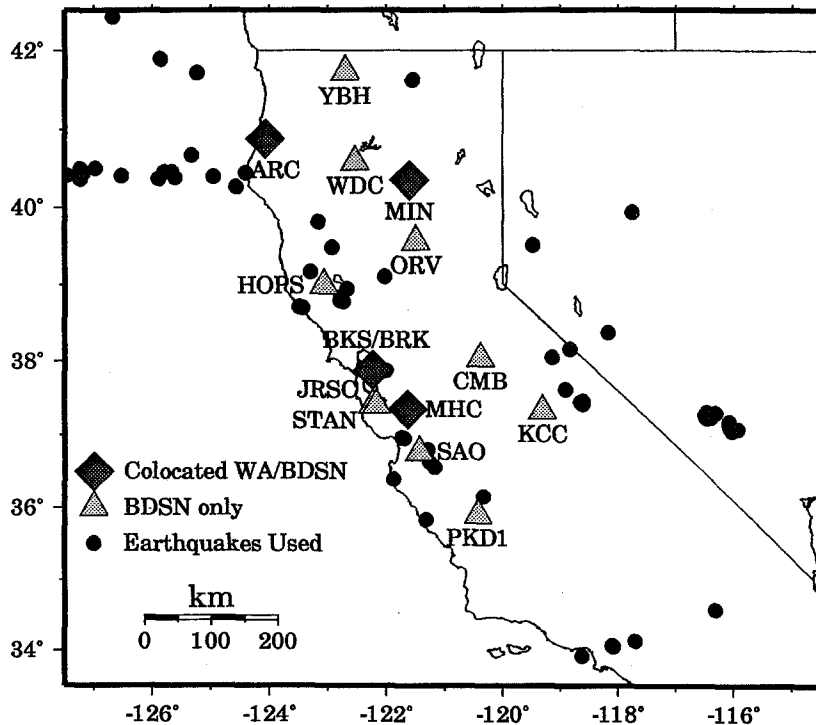


Figure 1. Map of California and vicinity showing the locations of the co-sited WA and BDSN broadband stations (diamonds), the rest of the BDSN stations (triangles), and the earthquakes (solid circles) used to verify the historical  $\delta M_L$ .

terworth filter with a 1.25-Hz corner frequency and a gain of 2080.

The routine procedure is to generate the SWA seismogram, by deconvolving the BDSN broadband signal to ground displacement and convolving the WA response (equation 2), and then to select the largest discrete sample amplitude for the “maximum trace amplitude” described by Richter (1935). We use the 80 samples/sec broadband channels (HHN and HHE), which have a 32-Hz bandwidth, for generating the SWA seismograms in order to minimize the discrete sampling error. It should be noted that we do not routinely remove the finite impulse response (FIR) antialias filter in the deconvolution process, which results in a small-frequency-dependent error, which is discussed in the next section. The 20 samples/sec broadband channels (BHN and BHE), which have an 8-Hz bandwidth, can also be used with the proviso that the “maximum trace amplitude” could be significantly underestimated.

### Comparison of SWA and WA Seismograms

BDSN broadband Streckeisen seismographs with 24-bit resolution Quanterra data loggers were co-sited at the four stations housing WA seismographs (ARC, BKS, MHC, and MIN) in order to compare the WA and SWA seismograms for local and regional events. Maximum trace amplitudes recorded on WA seismograms were measured using a 0.1-mm resolution comparator, measuring from the “zero” line of the trace to the midpoint of the trace at the maximum peak. Corresponding SWA records were generated from the co-sited BDSN records using the convolution procedure described in the previous section. Calculation of  $M_L$  using SWA seismograms requires that the “maximum trace amplitude,” but not necessarily the high-frequency detail, be accurately reproduced. Maximum trace amplitudes measured on numerous WA and corresponding SWA seismograms were compared, and a representative sample is given in Appendix C. From this comparison, we determined that the difference between the WA and SWA measured maximum trace amplitudes was not significant. This implies that the  $\delta M_L$  given in Table 2 is also appropriate for determining  $M_L$  from the SWA seismograms. The WA  $\delta M_L$  in Table 2 was thus adopted for determining  $M_L$  when using the SWA records.

Due to space limitations, a single WA seismogram was selected as representative for detailed analysis here. The selected ARC E–W component WA seismogram and the corresponding SWA seismogram are shown in Figure 3. Visual differences can immediately be seen between the two seismograms, particularly at the higher frequencies present in the coda. Note, however, that the maximum trace amplitudes registered by the two seismograms differ by less than 2%. This is fairly typical and representative of the differences between the WA and SWA seismograms we have compared. The implication is that we can reliably generate a SWA seismogram for the purpose of measuring the maximum trace amplitude.

A more detailed examination of the characteristics of the SWA seismogram is given in Figure 4. Note that the dominant frequency band associated with the maximum trace amplitude is approximately 4.5 to 6 Hz. At these frequencies, there are two competing error sources that act to bias the measured maximum trace amplitude. The first source is due to ignoring the FIR antialias filter (mentioned in the previous section), and the second source is due to the discrete sampling. The net result is that the log of the maximum trace amplitude, and hence the  $M_L$  estimate, can be in error by as much as  $\pm 0.015$  when the dominant frequencies are below  $\sim 7.5$  Hz. Above  $\sim 7.5$  Hz, the amplitudes will always be biased low, which also explains the observed differences between the WA and SWA high-frequency codas. It is fortuitous that the two error sources tend to cancel each other out at the dominant frequencies ( $< 7.5$  Hz) associated with the maximum trace amplitudes.

Visual comparisons between SWA and WA seismograms were encouraging, and we were interested in making a more quantitative study of the waveforms via coherency analysis. In order to make such a comparison, we scanned and digitized a number of WA seismograms recorded at ARC, BKS, MHC, and MIN. However, our results told us more about how well the WA records can be scanned and digitized than how well SWA replicate WA records. Two basic limitations were encountered, the physical resolution of the scanner and the high-frequency trace-following characteristics of the digitizer, which precluded digitization of the original WA seismograms with sufficient accuracy to be useful for coherency analysis. The scanner has a resolution of 400 dpi or  $\sim 15.8$  dots/mm. WA seismograms are recorded at a rate of 1 mm/sec; thus, spatial aliasing of the scanned image occurs at frequencies above  $\sim 7.8$  Hz. The trace-following algorithm, which produces the digitized record, does not reliably follow the scanned WA seismogram trace when large excursions at frequencies above  $\sim 2$  Hz are present. In an attempt to circumvent these limitations, we tried photographically enlarging the original WA seismogram by  $4\times$ , but sufficient trace detail was lost in the enlargement process that we were again thwarted.

### Inversion for BDSN $\delta M_L$ and $M_L$

Between 18 September 1992 and 6 September 1995, more than 14,000 SWA seismograms were generated for the purpose of determining  $M_L$  from the maximum trace amplitudes. This data set was reduced to 9148 SWA records by requiring that the earthquake be located within the western United States, that the maximum trace amplitudes be at least 0.05 for both components at each BDSN station recording the earthquake, and that at least two BDSN stations recorded the earthquake (the resulting events are shown in Fig. 2). The last requirement is so that  $M_L$  estimates can be differenced to eliminate the need to simultaneously determine the  $M_L$  of each event along with the  $\delta M_L$ 's for each BDSN station.

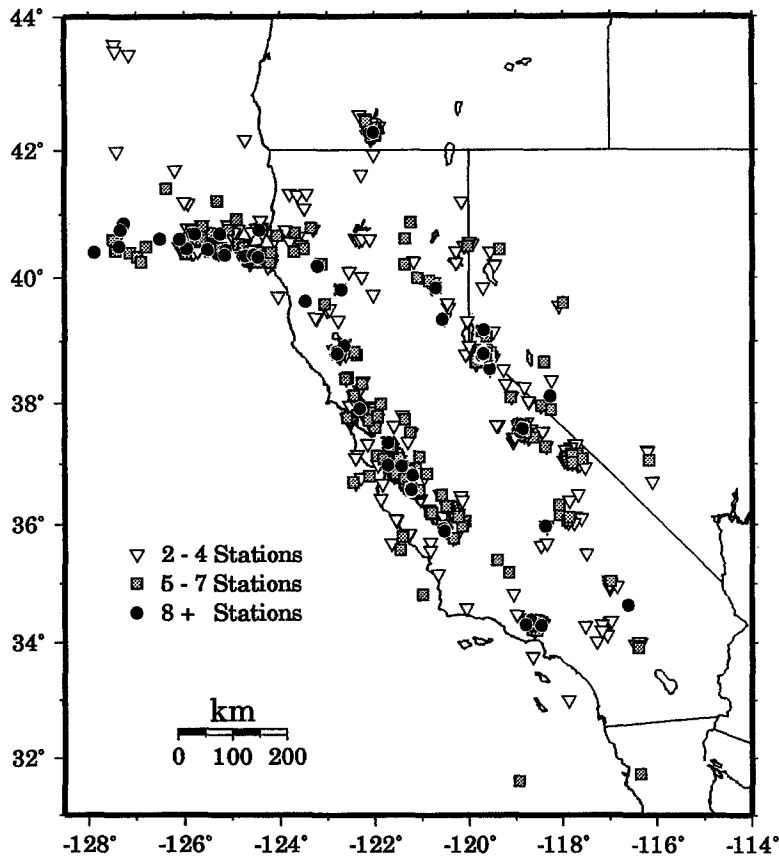


Figure 2. Map of California and vicinity showing the locations of the events used to determine the BDSN  $\delta M_L$  and  $-\log A_0(\Delta)$ . The different symbols indicate the number of BDSN stations that recorded the event. Inverted triangles, shaded squares, and solid circles represent 2 to 4, 5 to 7, and 8+ stations recording the event, respectively. Five events, either north of 44° latitude or east of 114° longitude, were omitted from the plot.

We solved for the BDSN  $\delta M_L$  using two methods: an “absolute” method where we solved simultaneously for the  $M_L$  of each event and the  $\delta M_L$  for each station, and a “differential” method where we solved for only the  $\delta M_L$  for each station by differencing the equations to eliminate the need to solve for the  $M_L$  of each event. For both methods, we constrained the  $\delta M_L$  for ARC, BKS, MHC, and MIN to the values given in Table 2 so that the  $\delta M_L$ , and hence the  $M_L$  of the events, would not be biased. After the initial inversions were done, observations with absolute  $M_L$  residuals larger than 0.6 were culled, and the inversions were repeated. The results are given in Table 3 (for both solutions) and Appendix D (for the “absolute” solution). Note that the  $\delta M_L$  results for the two methods are not significantly different. Subsequently, we adopted the average  $\delta M_L$  of the two solutions (as given in Table 3) for the routine BDSN determination of  $M_L$ . The resulting  $M_L$  residual distribution is shown in Figure 5. Note that the standard error is 0.201  $M_L$  units and that the residuals are approximately normally distributed. This standard error is essentially the same as the 0.203 standard error we obtained when determining  $M_L$  from the WA seismograms at the four original stations (ARC, BKS, MHC, and MIN) for events listed in Appendix A. The observation that the data variance does not change, when we switch from analog to digital determination of  $M_L$ , is also reassuring and an indication that the  $M_L$  estimation process is stationary.

#### Inversion for BDSN $-\log A_0(\Delta)$

In the process of analyzing the BDSN  $\delta M_L$ 's presented above, we discovered that the  $M_L$  residual distribution contained significant systematic differences as a function of distance, as shown in Figure 6. This is not surprising since Richter's attenuation function [ $-\log A_0(\Delta)$ ] is relevant to southern California, and this study encompasses a much larger region. Biases in the  $-\log A_0(\Delta)$  have been noted previously by Hutton and Boore (1987) for southern California and by Bakun and Joyner (1984) for central California, and they derived new attenuation functions for the two regions.

Since this study encompasses a much larger region, we decided to also invert for perturbations to  $-\log A_0(\Delta)$ . Several methods for parameterizing the perturbations to  $-\log A_0(\Delta)$  were tried systematically, and it was determined that a cubic spline with knots at 0, 25, 75, 150, and 300 km best fit the observed  $M_L$  residual pattern. Subsequently, we inverted for perturbations to  $-\log A_0(\Delta)$  with the additional imposed constraints that  $-\log A_0(\Delta = 100 \text{ km}) = 3.0$  (in agreement with Richter's definition) and that  $d[-\log A_0(\Delta = 0 \text{ km})]/d\Delta = 0$  (to avoid large perturbations where there is little data). The results are shown in Figure 7 and Table 4. The largest perturbations to  $-\log A_0(\Delta)$ , approaching +0.1 in amplitude, occur at distances less than 30 km and again around 200 km, and they are due to crustal structural

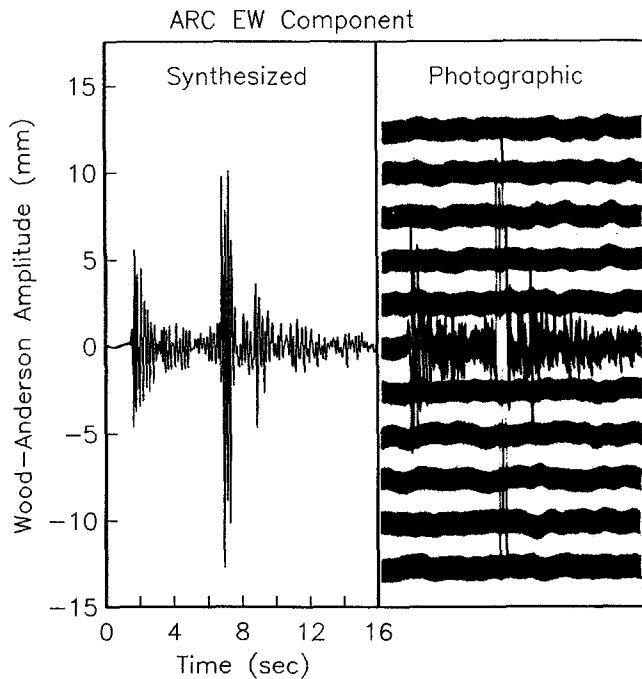


Figure 3. Comparison of the corresponding SWA and WA seismograms, recorded by the E-W component at ARC, for an  $M_L$  3.0 earthquake that occurred 30 km southwest of ARC. Note that while the maximum trace amplitude registered on the two records differ by less than 2%, the waveforms differ considerably in their high-frequency detail. These seismograms were chosen as representative of the comparisons that have been done.

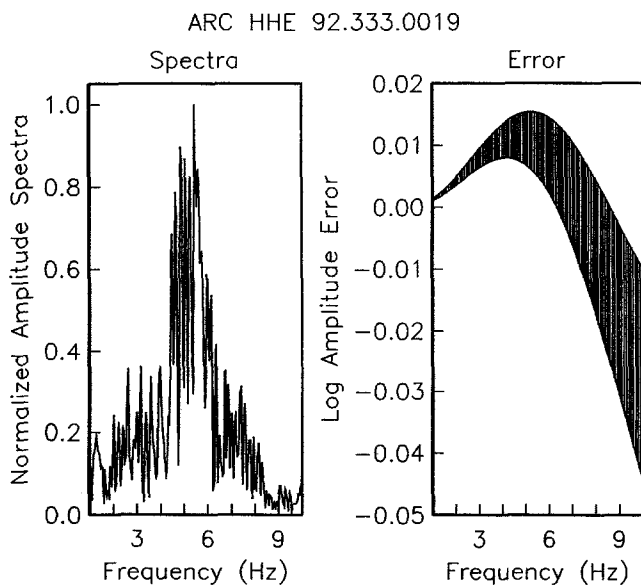


Figure 4. Amplitude spectrum for the SWA record shown in Figure 3 and estimates of the amplitude error range due to the discrete sampling (shaded range) and due to ignoring the FIR antialias filter response and the discrete sampling (curved shape of shaded region).

Table 3  
 $\delta M_L$  for the New BDSN Stations

Station	$\delta M_L^*$ (abs)	$\delta M_L^\dagger$ (diff)	$\delta M_L^\ddagger$ (avg)
CMB	$+0.237 \pm 0.0056$	$+0.243 \pm 0.007$	$+0.240 \pm 0.0090$
HOPS	$+0.329 \pm 0.0185$	$+0.318 \pm 0.026$	$+0.324 \pm 0.0319$
JRSC	$+0.142 \pm 0.0092$	$+0.131 \pm 0.013$	$+0.139 \pm 0.0159$
KCC <sup>§</sup>			$+0.39 \pm 0.105$
ORV	$+0.413 \pm 0.0067$	$+0.462 \pm 0.009$	$+0.428 \pm 0.0112$
PKD1	$-0.208 \pm 0.0076$	$-0.174 \pm 0.010$	$-0.198 \pm 0.0126$
SAO	$+0.308 \pm 0.0060$	$+0.327 \pm 0.007$	$+0.314 \pm 0.0092$
STAN	$-0.235 \pm 0.0105$	$-0.229 \pm 0.013$	$-0.233 \pm 0.0167$
WDC	$+0.457 \pm 0.0075$	$+0.516 \pm 0.009$	$+0.484 \pm 0.0117$
YBH	$+0.504 \pm 0.0095$	$+0.488 \pm 0.012$	$+0.499 \pm 0.0153$

\* $\delta M_L - \delta M_L$  derived from absolute inversion (including solving for  $M_L$ ).  
 † $\delta M_L - \delta M_L$  derived from differential inversion (without solving for  $M_L$ ).  
 ‡ $\delta M_L$ —adopted BDSN  $\delta M_L$  to be applied in determining BDSN  $M_L$  (average of  $\delta M_L^*$  and  $\delta M_L^\dagger$ ).  
 § $\delta M_L$  derived from Table 7 data.

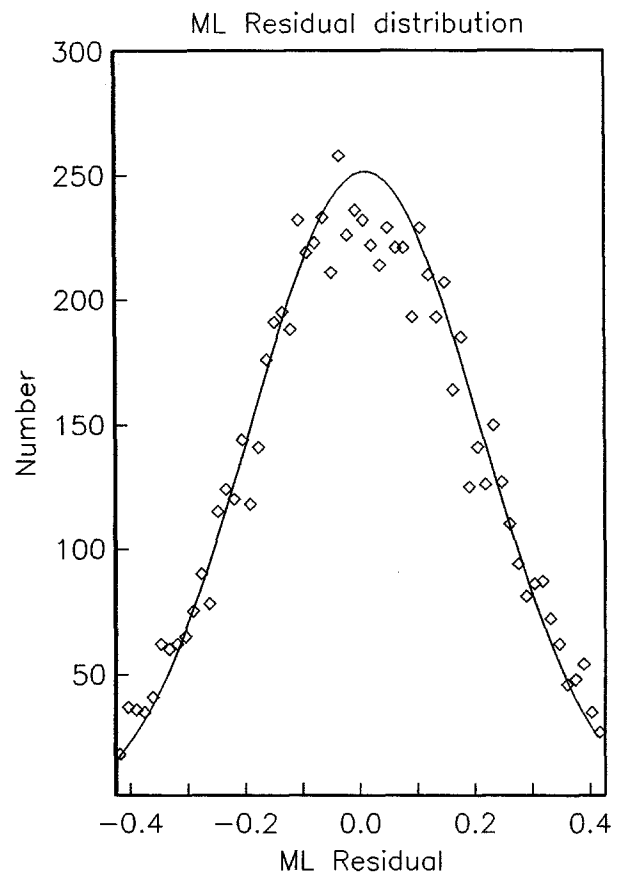


Figure 5.  $M_L$  residual histogram for the 9148 observations used in the inversion. The open diamonds are the number of observations, and the solid line is the least-squares fit normal distribution. The standard error of a single observation is 0.201  $M_L$  units.

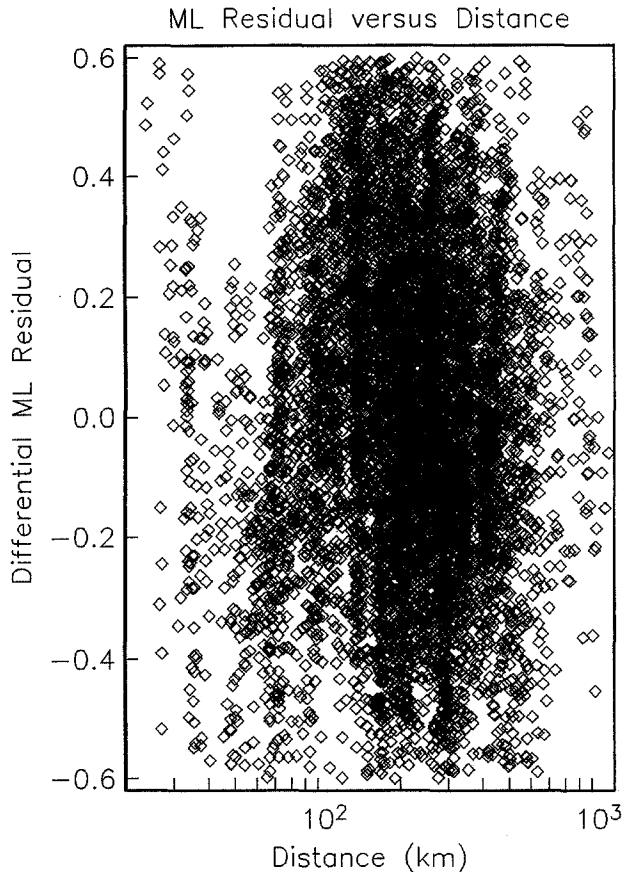


Figure 6. BDSN-derived  $M_L$  differential residual distribution versus distance. Note the significant structure in the scatter plot at distances less than 300 km, which implies that Richter's  $-\log A_0(\Delta)$  is biased for the much larger geographical region considered in this study.

differences between southern and northern California. Basically, the overall shape of  $-\log A_0(\Delta)$  is due to geometrical spreading and attenuation of the seismic wave field and the embayment in the 20- to 120-km range is due to amplification of the seismic wave field caused by internal crustal reflections. Using the BDSN-derived  $-\log A_0(\Delta)$  when determining  $M_L$  reduces the overall variance by 10%. However, in order to maintain continuity, we decided to employ Richter's  $-\log A_0(\Delta)$ , as given in Table 4, for routine BDSN determination of  $M_L$ .

#### Comparison with $M_w$ and other $M_L$ Estimates

A linear least-squares regression between the  $M_L$  determined here and the corresponding  $M_w$  determined from BDSN broadband waveform inversion (Pasyanos *et al.*, 1996) for 75 events ( $3.6 \leq M_L \leq 6.8$ ), listed in Appendix E and plotted in Fig. 8, is

$$M_w = (0.997 \pm 0.020) \cdot M_L - (0.050 \pm 0.131). \quad (3)$$

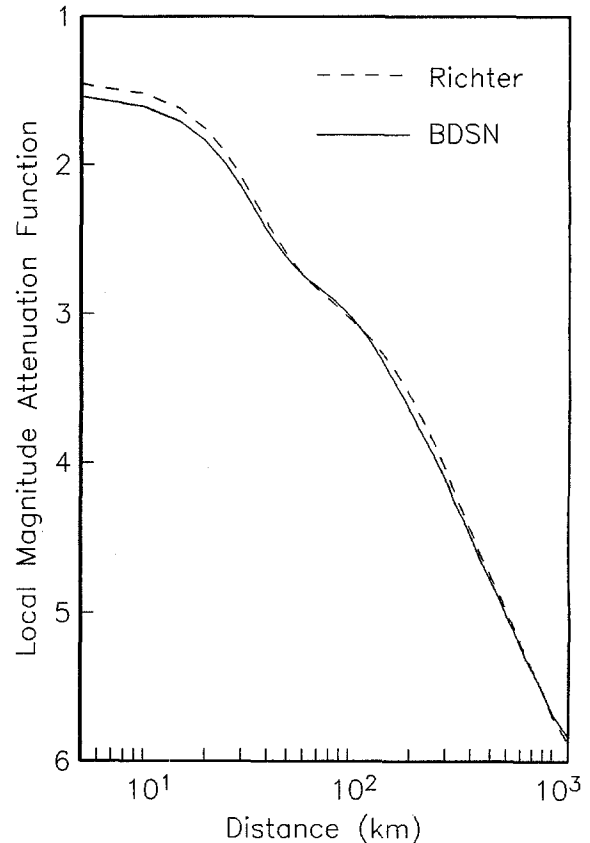


Figure 7. Comparison of  $-\log A_0(\Delta)$  for BDSN and Richter. Note that the largest differences are at distances less than 30 km and around 200 km. These differences are due in part to the higher resolution of this study and to variations in the crustal structure between northern California (this study) and southern California (Richter). The embayment in both curves in the 20- to 120-km range is caused by the crustal structure where internally reflected waves produce an amplification of the seismic wave field.

Since the uncertainties in  $M_w$  and  $M_L$ , given in Appendix E, are of the same order, the regression was done bilinearly to minimize the normal distance between the sample points and the regression line. Within the uncertainties in the regression,  $M_w \approx M_L$ . Equation (3) is consistent with the results of Hanks and Kanamori (1979).

A comparison of  $M_L$  determined here with the corresponding  $M_L$  determined using TERRASCOPE stations (H. Kanamori, personal comm., 1995) is given in Table 5 for 10 recent earthquakes. The average difference between the two  $M_L$  estimates (TERRASCOPE - BDSN) is  $-0.084 \pm 0.053$ , which is not significant. Thus, there is no evidence for a systematic bias between the two  $M_L$  estimates.

A comparison of  $M_L$  determined here with the corresponding  $M_L$  determined by University of Nevada, Reno (UNR) (Savage and Anderson, 1995), is given in Table 6 for 10 recent earthquakes. The average difference between the two  $M_L$  estimates (UNR - BDSN) is  $-0.42 \pm 0.064$ , which

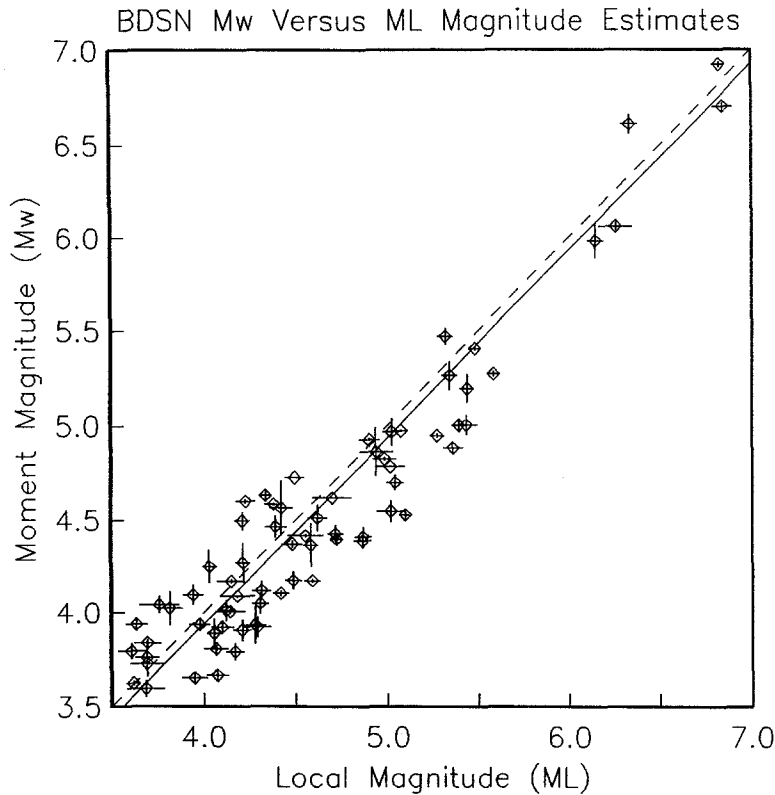


Figure 8. Comparison of  $M_L$  and  $M_w$ , both derived from the BDSN broadband data. A least-squares fit to the data (regressed on both axes because the uncertainties are of the same order) is given by the solid line. Note that the regression demonstrates that  $M_L$  and  $M_w$  are not significantly different over the  $3.6 \leq M_L \leq 6.8$  range. A dashed line running through the origin with unity slope is given for comparison. The  $M_w$  data are the average of the  $M_w$ 's determined by body waveform inversion and by surface waveform inversion (Pasyanos *et al.*, 1996). The data are given in Appendix E.

is quite significant. Thus, on average, the UNR-determined  $M_L$  are 0.4 smaller than the corresponding BDSN-determined  $M_L$ . This bias has been noted previously (Evernden, 1975), and the difference between magnitudes is not explained by average attenuation differences and is in need of further study (M. K. Savage, personal comm., 1996).

#### Prediction of $\delta M_L$

The wide range of the BDSN  $\delta M_L$ 's from  $-0.2$  at soft alluvial sites to  $+0.5$  at hard-rock sites led to the question of whether or not  $\delta M_L$  could be reliably predicted from the site characteristics. The two most obvious site characteristics that could influence  $\delta M_L$  are the average rigidity ( $\mu$ ) of the rock and the average curvature ( $\kappa$ ) of the local terrain in the vicinity of the station. Subsequently, we estimated the average  $\mu$  of the bedrock lithology from geologic maps (Jennings, 1969) and the physical properties of rocks (Carmichael, 1989), as given in Table 1. We also estimated the average  $\kappa$  of the local terrain within a 500-m radius of the site by fitting a three-dimensional quadric surface through high-resolution digitized terrain data (Edwards and Batson, 1990) and determined the average  $\kappa$  at the site, as also given in Table 1. A least-squares regression of  $\log \mu$  and  $\kappa$  to the  $\delta M_L$  data (see Fig. 9) gives the following:

$$\delta M_L = (0.597 \pm 0.032) \cdot \log \mu + (0.025 \pm 0.018) \cdot \kappa, \quad (4)$$

where  $\mu$  is in units of  $10^{11}$  dynes/cm<sup>2</sup> and  $\kappa$  is in units of

km<sup>-1</sup>. The result is that  $\delta M_L$  for a station can basically be predicted from knowledge of the average  $\mu$  of the site, and  $\delta M_L$  is relatively insensitive to average  $\kappa$  of the local terrain.

When we initially regressed  $\delta M_L$  against  $\mu$  and  $\kappa$ , BKS and MHC were the largest outliers, both being more than  $+0.2$ . This was puzzling, and, subsequently, it was determined (David L. Jones, personal comm., 1995) that the surface rocks at both BKS and MHC ( $\mu$  given in parenthesis in Table 1) are very thin (perhaps less than 200 m), and, at both sites, the subsurface rocks have a lower  $\mu$ . At the dominant frequencies ( $\sim 5$  Hz, say) and corresponding wavelengths ( $\sim 140$  m, say) associated with maximum trace amplitudes (see Fig. 4), the surface rocks are basically transparent to the seismic wave field, and the  $\delta M_L$  is primarily influenced by  $\mu$  of the subsurface rocks. Eaton (1992) also found that  $\delta M_L$  varies systematically with bedrock lithology. Thus the subsurface  $\mu$  values, given in Table 1 for BKS and MHC, were adopted for all subsequent calculations.

As a test, we used data from the newest BDSN station at Kaiser Creek (KCC) (see Table 1) that became operational on 8 December 1995. KCC is sited in a 1000-ft tunnel excavated in solid granite in the Sierra Nevada with an estimated  $\mu$  of  $3.4 \cdot 10^{11}$  dynes/cm<sup>2</sup> and, from equation (4), a predicted  $\delta M_L$  of  $+0.36$ . Subsequently, we extracted broadband KCC data for several recent earthquakes, as shown in Table 7. Comparing the KCC-determined  $M_L$  with the  $M_L$  determined from the rest of the BDSN stations, we see that  $\delta M_L = +0.39 \pm 0.103$  for KCC, which is in agreement with the above prediction.



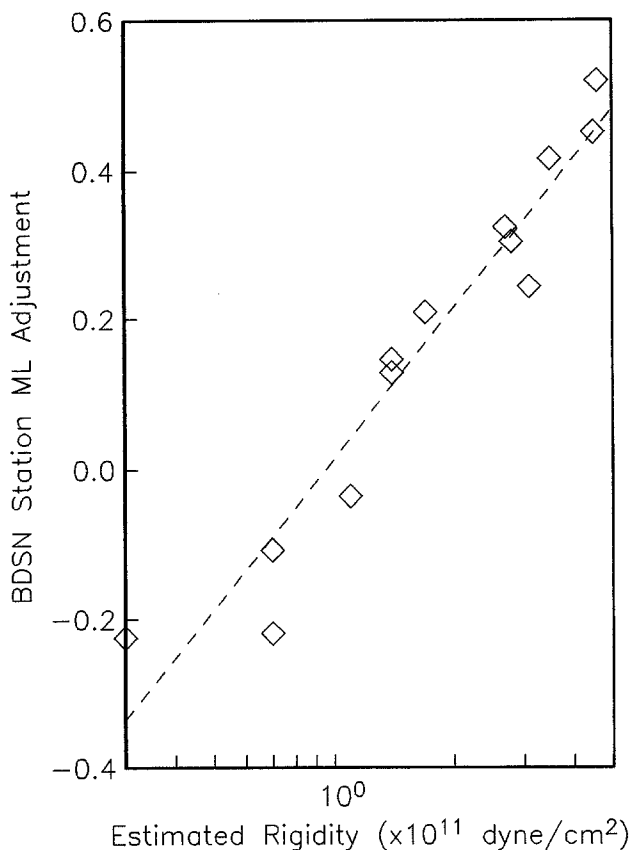


Figure 9. Comparison of the BDSN  $\delta M_L$  and the estimated average  $\mu$  of the surrounding rock. The open diamonds are the BDSN station data, and the dashed line is the least-squares fit of the  $\delta M_L$ 's and the estimated  $\mu$  for each station. Note that the  $\delta M_L$  is approximately  $0.6 \cdot \log(\mu)$  (equation 4), so we can predict  $\delta M_L$  to within approximately  $\pm 0.1$  for a station if we have knowledge of the average  $\mu$  of the surrounding rock to an accuracy of  $\pm 50\%$ .

Conclusions

We can successfully generate SWA seismograms, for the purpose of measuring the maximum trace amplitudes, using a basic convolution procedure that ignores the effects of the FIR antialias filter and the sampling error inherent in discrete sampling. We recommend that 80-samples/sec data be utilized when generating SWA seismograms. However, lower sampling rates can also be utilized without excessive loss of accuracy as long as the frequencies associated with the maximum trace amplitudes are below approximately 1/10 of the sampling rate.

We can indeed produce a seamless Berkeley  $M_L$  catalog when changing from WA to SWA seismogram measurement of the maximum trace amplitudes by utilizing the average BDSN  $\delta M_L$ 's listed in Tables 2 and 3 and Richter's  $-\log A_0(\Delta)$  given in Table 4. Utilizing the BDSN  $-\log A_0(\Delta)$  (Table 4) reduces the variance by 10%. However, we decided to use Richter's  $-\log A_0(\Delta)$  in order to maintain continuity in the Berkeley  $M_L$  catalog since the BDSN  $-\log$

Table 4  
BDSN  $-\log A_0(\Delta)$

$\Delta$	$-\log A_0^*$	$-\log A_0^\dagger$	$\Delta$	$-\log A_0^*$	$-\log A_0^\dagger$
0	1.4	1.489	260	3.8	3.933
5	1.4	1.489	270	3.9	3.976
10	1.5	1.588	280	3.9	4.020
15	1.6	1.685	290	4.0	4.063
20	1.7	1.782	300	4.0	4.107
25	1.9	1.976	310	4.1	4.151
30	2.1	2.168	320	4.1	4.195
35	2.3	2.359	330	4.2	4.240
40	2.4	2.448	340	4.2	4.278
45	2.5	2.537	350	4.3	4.311
50	2.6	2.625	360	4.3	4.344
55	2.7	2.713	370	4.3	4.378
60	2.8	2.744	380	4.4	4.412
65	2.8	2.776	390	4.4	4.446
70	2.8	2.809	400	4.5	4.480
80	2.9	2.870	410	4.5	4.515
85	2.9	2.901	420	4.5	4.549
90	3.0	2.934	430	4.6	4.584
95	3.0	2.969	440	4.6	4.619
100	3.0	3.000	450	4.6	4.649
110	3.1	3.064	460	4.6	4.674
120	3.1	3.132	470	4.7	4.699
130	3.2	3.203	480	4.7	4.725
140	3.2	3.272	490	4.7	4.750
150	3.3	3.341	500	4.7	4.775
160	3.3	3.407	510	4.8	4.800
170	3.4	3.470	520	4.8	4.826
180	3.4	3.530	530	4.8	4.851
190	3.5	3.589	540	4.8	4.877
200	3.5	3.645	550	4.8	4.902
210	3.6	3.699	560	4.9	4.927
220	3.65	3.751	570	4.9	4.952
230	3.7	3.798	580	4.9	4.978
240	3.7	3.844	590	4.9	5.003
250	3.8	3.889	600	4.9	5.028

\*Richter's  $-\log A_0(\Delta)$  ( $\Delta$  in km) from Table 22-1 in Richter (1958).

†BDSN  $-\log A_0(\Delta)$ . For  $\Delta \geq 600$  km, use  $-\log A_0(\Delta) = 2.9492 \cdot \log(\Delta) - 3.1753$ .

$A_0(\Delta)$  is a potential source of bias when comparing the current BDSN SWA-derived  $M_L$  with the Berkeley  $M_L$  published over the past five decades.

A linear regression of  $M_w$  versus  $M_L$  determined using BDSN broadband records shows that  $M_w$  and  $M_L$  track each other over at least the  $3.6 \leq M_L \leq 6.8$  range. A comparison between the BDSN- and TERRAScope-determined  $M_L$  indicates that they are not significantly different. A similar comparison between the BDSN-determined  $M_L$  and the corresponding UNR-determined  $M_L$  indicates a significant difference in that the UNR  $M_L$  is  $0.42 \pm 0.064$  smaller. This difference in magnitude cannot be explained solely by differences in  $-\log A_0(\Delta)$  between California and the western Great Basin.

The  $\delta M_L$  for a new BDSN station can be predicted within

**Table 5**  
Comparison of BDSN and TERRAScope-Determined  $M_L$

Date/Time	$M_L \pm \sigma$ (BDSN)	$M_L^* \pm \sigma$ (TERRA)	Diff†	$M_w \ddagger$ (BDSN)	$M_E \ddagger \pm \sigma$ (TERRA)
93.042.1239	4.50 ± 0.062	4.26 ± 0.36	-0.24		4.23 ± 0.25
93.137.2320	6.26 ± 0.088	6.25 ± 0.21	-0.01	6.06	6.52 ± 0.21
93.140.2014	4.89 ± 0.042	4.60 ± 0.13	-0.29	4.60	4.52 ± 0.11
93.148.0447	5.02 ± 0.078	5.19 ± 0.18	+0.17	4.79	5.01 ± 0.10
94.079.2120	5.35 ± 0.040	5.37 ± 0.18	+0.02	5.26	5.35 ± 0.12
95.050.2124	4.68 ± 0.056	4.33 ± 0.23	-0.35		4.25 ± 0.17
95.064.0007	4.60 ± 0.043	4.66 ± 0.24	+0.06	4.17	4.40 ± 0.19
95.064.0248	4.43 ± 0.048	4.35 ± 0.24	-0.08	3.97	4.13 ± 0.21
95.127.1103	5.05 ± 0.046	4.99 ± 0.11	-0.06	4.66	4.92 ± 0.07
95.177.0840	5.22 ± 0.038	5.13 ± 0.21	-0.09	4.96	5.05 ± 0.14

\*TERRAScope-determined  $M_L$ .

† $M_L$  difference (TERRAScope - BDSN). The average difference is  $-0.084 \pm 0.053$ .

‡BDSN  $M_w$  and TERRAScope  $M_E$  (Kanamori, 1993) for comparison.

**Table 6**  
Comparison of BDSN- and UNR-Determined  $M_L$

Date/Time	$M_L \pm \sigma$ (BDSN)	$M_L$ (UNR)	Diff*	$M_w$ (BDSN)	$M_c \ddagger$ (UNR)
93.041.2148	5.03 ± 0.050	4.80	-0.23	4.55	4.59
93.062.1530	3.49 ± 0.093	2.93	-0.56		3.79
93.087.0734	3.91 ± 0.041	3.91	0.00		3.52
93.110.2116	3.35 ± 0.059	2.76	-0.59		3.48
93.119.1222	3.62 ± 0.062	3.03	-0.59		3.47
93.137.2320	6.26 ± 0.088	5.90	-0.36	6.06	6.1
93.137.2336	5.04 ± 0.055	4.37	-0.67		4.38
93.137.2342	4.36 ± 0.069	4.01	-0.35		3.48
93.140.0117	4.39 ± 0.061	3.88	-0.51	4.34	3.94
93.150.1521	4.10 ± 0.107	3.75	-0.35		4.27

\* $M_L$  difference (UNR - BDSN). The average difference is  $-0.42 \pm 0.064$ .

‡Coda duration magnitude (Lee *et al.*, 1972) given for comparison.

a tenth from the average  $\mu$  of the rock (or alluvium) on which the station is sited.  $\delta M_L$  ranges from approximately  $-0.2$  on the softest alluvial sites to approximately  $+0.5$  on the hardest-rock sites.

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syanos provided their BDSN-derived  $M_w$ 's for comparison. This is Seismographic Station Contribution Number 96-05.

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Table 7  
KCC  $\delta M_L$

Date/Time	$\Delta$ (km)	Az (deg)	$M_L^* \pm \sigma$ (BDSN)	$M_L^\dagger \pm \sigma$ (KCC)	$\delta M_L^\ddagger$
95.347.0545	195.7	259.3	$3.99 \pm 0.047$	$3.89 \pm 0.162$	+0.10
95.347.0619	195.5	259.9	$3.53 \pm 0.029$	$3.36 \pm 0.159$	+0.17
95.347.0625	194.9	259.7	$4.05 \pm 0.026$	$4.03 \pm 0.130$	+0.02
95.351.0520	349.4	299.3	$3.17 \pm 0.048$	$3.30 \pm 0.086$	-0.13
95.356.0900	160.7	351.1	$5.24 \pm 0.045$	$4.53 \pm 0.050$	+0.71
95.357.0539	155.6	349.9	$5.16 \pm 0.042$	$4.63 \pm 0.070$	+0.53
95.361.0810	141.2	320.1	$2.70 \pm 0.060$	$1.93 \pm 0.090$	+0.77
95.362.1828	158.0	349.2	$5.48 \pm 0.043$	$4.87 \pm 0.015$	+0.61
95.362.2005	156.5	349.7	$3.10 \pm 0.121$	$2.32 \pm 0.011$	+0.78
96.002.0626	157.9	349.5	$4.13 \pm 0.049$	$3.28 \pm 0.074$	+0.85
96.007.1433	227.7	139.7	$5.34 \pm 0.029$	$4.70 \pm 0.063$	+0.66
96.011.0258	167.2	228.9	$3.08 \pm 0.064$	$3.28 \pm 0.056$	-0.20
96.011.1706	146.0	230.0	$3.21 \pm 0.093$	$2.97 \pm 0.113$	+0.24

\* $M_L$  derived using all BDSN stations but KCC.

† $M_L$  derived using only KCC.

‡ $\delta M_L$  (BDSN - KCC) to be added to  $M_L$  estimate from KCC (equation 1). The average KCC  $\delta M_L = +0.39 \pm 0.103$ .

Appendix A  
WA Data Used to Verify Historical  $\delta M_L$

Date	Time	Lat	Long	$M_L \pm \sigma$	ARC*		BKS*		MHC*		MIN*	
					N	E	N	E	N	E	N	E
84/01/23	05:40	36.39	-121.88	$5.07 \pm 0.073$	0.90	1.10	104.00	82.00	64.00	66.30	2.50	3.10
84/02/16	11:14	39.93	-117.76	$5.18 \pm 0.072$	2.00	1.40	3.10	3.80	6.40	3.50	7.90	5.60
84/02/28	15:16	40.36	-125.90	$5.16 \pm 0.122$	34.60	40.00	2.40	2.80	1.20	1.10	30.30	30.70
84/03/01	17:45	37.07	-116.05	$5.52 \pm 0.061$	0.70	0.90	4.10	4.30	11.00	6.00	2.00	3.60
84/04/28	22:48	37.62	-118.91	$4.66 \pm 0.100$	0.30	0.30	3.10	3.30	6.00	2.70	9.00	3.90
84/05/31	13:04	37.10	-116.05	$5.55 \pm 0.047$	0.60	0.60	5.00	4.00	10.00	7.40	4.50	4.00
84/07/25	15:30	37.27	-116.41	$5.35 \pm 0.078$	0.50	0.70	2.10	2.40	7.40	11.80	2.60	2.40
84/08/04	21:45	40.26	-124.58	$4.70 \pm 0.078$	44.40	40.80	2.10	1.90	1.10	0.80	19.00	21.70
84/09/10	07:47	40.41	-127.46	$4.46 \pm 0.077$	0.70	0.90	0.50	0.50	0.30	0.30	1.10	0.80
84/09/10	23:52	40.36	-127.24	$4.67 \pm 0.086$	1.40	1.60	0.80	1.20	0.80	0.50	1.70	1.20
84/09/11	11:23	40.49	-127.23	$4.62 \pm 0.095$	1.20	1.30	0.80	0.80	0.80	0.50	1.40	1.30
84/09/20	18:30	40.38	-125.62	$4.83 \pm 0.133$	17.60	28.20	1.20	1.60	0.50	0.60	16.70	21.20
84/09/20	19:04	40.43	-127.19	$4.84 \pm 0.049$	3.60	4.90	0.80	0.90	0.70	0.70	2.80	3.10
84/11/23	18:08	37.46	-118.61	$6.12 \pm 0.060$	12.40	12.00	65.00	72.00	104.60	91.40	60.50	82.20
84/11/23	19:12	37.42	-118.61	$5.54 \pm 0.046$	1.70	1.50	16.50	16.00	46.60	61.90	16.90	18.80
84/11/26	16:21	37.45	-118.65	$5.63 \pm 0.043$	3.40	1.90	27.50	20.00	71.20	71.30	15.10	17.40
85/01/07	06:17	40.40	-126.53	$4.85 \pm 0.107$	8.50	5.90	1.50	1.30	0.70	0.35	5.50	10.40
85/01/24	11:27	38.16	-118.84	$5.20 \pm 0.069$	1.00	0.90	23.30	22.80	26.40	13.10	7.30	14.20
85/03/06	01:52	38.95	-122.68	$3.52 \pm 0.077$	0.30	0.50	4.60	3.70	0.60	0.50	0.90	1.30
85/03/23	18:30	37.18	-116.08	$5.13 \pm 0.069$	0.30	0.40	2.00	1.60	4.80	3.00	1.10	0.90
85/04/18	16:29	39.11	-122.03	$3.70 \pm 0.088$	0.60	0.70	2.80	1.80	0.80	0.50	4.40	8.10
85/05/12	13:55	40.39	-124.96	$4.32 \pm 0.096$	6.90	8.90	0.80	0.80	0.35	0.35	9.40	6.00
85/05/28	07:56	39.51	-119.48	$4.34 \pm 0.034$	0.30	0.30	1.75	2.25	2.20	2.00	7.40	7.80
85/12/05	15:00	37.05	-116.04	$5.34 \pm 0.074$	0.60	0.40	2.90	2.10	8.00	6.10	1.50	1.80
86/02/11	01:15	41.72	-125.25	$4.92 \pm 0.048$	47.40	38.50	1.40	0.95	0.70	0.55	6.40	8.50

(continued)

Appendix A (Continued)

Date	Time	Lat	Long	$M_L \pm \sigma$	ARC*		BKS*		MHC*		MIN*	
					N	E	N	E	N	E	N	E
86/05/31	08:47	36.63	-121.27	4.65 ± 0.052	0.30	0.30	33.80	22.60	45.40	57.30	1.40	1.50
86/06/25	20:27	37.27	-116.50	5.39 ± 0.043	0.70	0.70	3.80	3.60	9.60	4.40	3.10	3.10
86/10/12	06:43	38.72	-123.50	3.96 ± 0.081	2.10	1.10	6.30	5.90	1.80	1.10	0.80	1.60
86/10/16	19:25	37.22	-116.46	5.40 ± 0.062	0.60	0.90	5.30	4.20	9.70	4.00	2.80	2.20
86/11/14	16:00	37.10	-116.05	5.55 ± 0.047	0.60	1.00	5.30	4.50	9.00	6.70	3.80	2.80
87/02/14	07:26	36.15	-120.33	5.29 ± 0.086	0.80	1.10	22.00	19.50	51.30	33.40	12.30	11.80
87/04/16	04:52	40.44	-124.41	4.17 ± 0.105	20.60	41.90	0.30	0.40	0.30	0.30	5.90	7.00
87/04/30	13:30	37.23	-116.42	5.36 ± 0.038	0.60	0.60	3.50	3.00	7.40	5.40	2.40	3.50
87/05/01	22:22	39.81	-123.17	3.78 ± 0.094	5.90	4.30	0.70	0.50	0.40	0.30	4.30	4.80
87/07/28	18:55	38.38	-118.17	4.60 ± 0.046	0.40	0.30	2.60	2.10	2.10	1.60	1.70	2.50
87/08/13	14:00	37.08	-115.93	5.60 ± 0.061	1.00	1.40	4.50	4.30	12.50	4.80	2.90	3.40
87/10/01	14:42	34.06	-118.08	6.07 ± 0.044	1.90	2.20	10.50	12.00	15.90	15.30	8.10	12.60
87/10/04	10:59	34.07	-118.10	5.58 ± 0.045	0.80	0.60	4.40	3.60	8.10	3.70	2.80	3.10
87/10/23	16:00	37.14	-116.08	5.17 ± 0.045	0.40	0.50	1.40	1.30	3.60	3.10	1.40	1.60
88/02/15	18:10	37.31	-116.47	5.28 ± 0.079	1.10	1.00	2.20	2.90	5.00	3.70	1.50	1.80
88/02/20	08:39	36.80	-121.30	5.09 ± 0.064	1.00	0.80	103.50	82.30	130.60	100.10	8.00	9.00
88/07/16	05:23	39.17	-123.30	3.64 ± 0.043	0.90	0.80	1.60	1.20	1.00	0.70	1.10	1.50
88/07/26	03:26	36.56	-121.18	4.59 ± 0.048	0.40	0.60	14.70	11.20	30.50	21.60	1.50	1.70
88/08/30	18:00	37.09	-116.07	5.09 ± 0.079	0.60	0.50	0.90	0.80	3.40	2.00	1.20	1.10
88/09/30	00:30	41.63	-121.55	4.27 ± 0.035	3.00	2.20	0.40	0.40	0.50	0.30	14.10	14.00
88/10/13	14:00	37.09	-116.03	5.65 ± 0.053	1.10	1.10	5.70	5.20	15.00	6.80	4.30	3.50
88/10/20	17:33	38.80	-122.80	3.66 ± 0.120	0.70	0.70	8.80	5.30	1.30	1.00	0.60	0.50
88/10/25	14:43	38.71	-123.44	3.82 ± 0.067	0.70	0.60	7.10	5.00	1.50	1.20	0.70	1.10
89/01/19	06:53	33.92	-118.63	5.27 ± 0.019	0.35	0.30	2.40	2.40	3.80	2.90	1.40	1.10
89/05/04	03:37	40.57	-127.54	4.63 ± 0.075	1.10	1.30	0.60	0.80	0.40	0.35	1.50	1.40
89/06/22	21:15	37.28	-116.41	5.29 ± 0.043	0.35	0.55	2.80	2.80	6.90	4.40	2.75	2.80
89/08/08	23:15	39.48	-122.93	4.08 ± 0.135	7.40	7.70	1.60	1.50	0.80	0.65	10.55	16.20
89/12/08	15:00	37.23	-116.41	5.26 ± 0.052	0.40	0.45	2.80	2.50	6.70	4.70	1.65	2.80
90/01/06	05:35	40.45	-125.67	4.30 ± 0.054	6.10	5.00	0.70	0.40	0.30	0.30	2.40	2.50
90/01/27	22:06	38.79	-122.74	3.52 ± 0.160	0.30	0.35	13.00	9.30	0.75	0.60	0.40	0.35
90/02/28	23:43	34.14	-117.70	6.21 ± 0.039	2.55	2.00	14.80	11.00	27.40	28.00	11.80	14.50
90/04/03	21:12	38.84	-122.79	3.63 ± 0.147	0.70	0.65	9.00	9.00	0.80	1.00	0.40	0.50
90/04/18	15:46	36.95	-121.70	5.06 ± 0.087	2.35	1.50	123.00	141.00	156.00	132.00	6.90	8.00
90/04/28	04:47	37.87	-122.01	4.22 ± 0.084	0.40	0.70	135.70	148.60	45.00	39.00	2.00	3.20
90/06/13	16:00	37.26	-116.42	5.63 ± 0.047	1.10	1.50	5.60	7.10	14.80	9.10	4.80	4.50
90/07/31	03:19	42.42	-126.68	5.06 ± 0.082	6.00	7.10	1.30	1.00	1.00	1.20	1.60	1.40
90/09/26	04:14	40.45	-125.80	4.66 ± 0.123	14.50	16.00	0.80	0.80	0.40	0.30	10.00	10.00
90/10/03	12:57	40.50	-126.98	4.37 ± 0.105	1.50	1.10	0.40	0.40	0.60	0.70	0.50	0.40
90/10/12	17:30	37.25	-116.49	5.54 ± 0.061	2.00	1.30	4.00	3.60	10.50	6.00	4.00	5.00
90/10/24	06:15	38.05	-119.15	5.82 ± 0.050	7.20	7.60	68.70	58.50	67.00	97.00	71.00	86.00
90/12/07	21:51	40.67	-125.33	4.51 ± 0.076	7.60	17.40	0.80	0.70	0.70	0.50	6.90	5.00
91/03/24	03:42	36.96	-121.74	4.55 ± 0.059	0.50	0.30	39.60	33.10	67.50	66.50	2.50	3.00
91/04/04	19:00	37.30	-116.31	5.31 ± 0.089	0.40	0.30	4.10	3.00	10.50	6.50	1.80	2.00
91/04/16	15:30	37.24	-116.44	5.39 ± 0.074	0.40	0.60	3.70	3.90	13.00	7.50	2.50	3.00
91/07/13	06:09	41.89	-125.87	4.79 ± 0.062	5.90	9.00	0.80	0.70	0.60	0.60	3.40	5.50
91/09/17	21:10	35.83	-121.32	5.14 ± 0.053	0.80	1.10	36.00	27.10	50.00	41.20	1.70	2.80
92/07/05	21:18	34.58	-116.32	5.72 ± 0.039	0.80	1.20	3.50	2.80	5.60	4.60	3.10	2.80

\*WA maximum trace amplitude (A) in mm.  
The standard error is 0.203  $M_L$  units.

Appendix B  
Calibration Parameters for the WA Seismographs

Station	Component*	$V_S^\dagger$	$T_S^\dagger$ (sec)	$h_S^\dagger$	Instrument‡
ARC	S-N	2080	0.81	0.75	LG
	E-W	1920	0.81	0.66	LG
BKS	S-N	2060	0.80	0.66	LG
	W-E	2110	0.80	0.71	LG
MHC	S-N	2010	0.80	0.70	H
	E-W	2030	0.77	0.71	H
MIN	N-S	2010	0.80	0.69	H
	E-W	2190	0.79	0.74	H

\*Component is given in terms of up-down on the WA seismogram.

† $V_S$  = static magnification,  $T_S$  = free period, and  $h_S$  = fraction of critical damping of standard Wood-Anderson torsion seismograph.

‡Manufacturer; H = Henson and LG = Lehner and Griffith.

The above calibration parameters were determined within the last year of operation of the instruments. The scatter around the adopted values of  $V_S = 2080$ ,  $T_S = 0.8$ , and  $h_S = 0.7$  is typical. Note that the average  $V_S = 2050 \pm 30$ , which is not significantly different than the adopted  $V_S$  value of  $2080 \pm 60$ . For details about the WA calibration procedure, see Appendix A in Uhrhammer and Collins (1990).

Appendix C  
SWA and WA Maximum Trace Amplitude Comparison

Date	Time	Lat.	Lon.	Stn	Diff*
91/09/11	01:30	37.00	-121.94	MHC	+0.064
91/09/19	09:07	36.88	-121.66	MHC	+0.042
91/09/19	09:07	36.88	-121.66	BKS	-0.083
91/09/21	14:31	37.48	-121.81	MHC	+0.024
91/10/07	12:11	37.53	-121.39	MHC	+0.064
91/12/14	08:12	37.40	-121.75	MHC	-0.067
92/01/21	03:56	37.42	-121.70	MHC	-0.086
92/02/15	14:36	37.69	-121.59	BKS	-0.081
92/04/23	04:50	33.96	-116.32	MHC	+0.067
92/04/23	23:10	37.36	-121.69	MHC	+0.072
92/04/26	07:41	40.45	-124.63	MHC	+0.035
92/10/20	05:28	35.92	-120.49	MHC	+0.015
92/10/31	17:00	36.80	-121.54	MHC	+0.081
92/11/23	20:59	38.08	-121.86	BKS	+0.048
92/11/27	16:00	34.34	-116.90	MHC	-0.058
92/12/26	22:11	43.93	-127.89	ARC	-0.017
93/05/18	23:48	37.06	-117.86	MIN	-0.031
93/05/19	14:13	37.13	-117.78	MIN	+0.017

\* $M_L$  difference (SWA - WA).

Note that the average  $M_L$  difference ( $+0.005 \pm 0.014$ ) is not significant, which implies that the WA- and SWA-determined maximum trace amplitudes are, on average, the same. The observed 0.0035 variance of the  $M_L$  differences is consistent with the variance due to the scatter in the  $V_S$  of the individual WA seismographs (see Appendix B) and due to the errors caused by the FIR filter and discrete sampling (see Fig. 4). Therefore, we adopt the WA  $\delta M_L$  from this study (given in Table 2) to determine  $M_L$  from the SWA maximum trace amplitudes.





Appendix E  
 BDSN  $M_w$  and  $M_L$  Comparison

Date/Time	Lat	Long	$M_w \pm \sigma$	$M_L \pm \sigma$	Location
93.016.0629	37.03	-121.46	5.01 ± 0.050	5.45 ± 0.064	Gilroy
93.041.2148	40.40	-119.58	4.55 ± 0.058	5.03 ± 0.075	Pyramid Lake
93.094.0521	35.95	-120.51	4.47 ± 0.059	4.40 ± 0.061	Parkfield
93.137.2320	37.16	-117.69	6.06 ± 0.021	6.26 ± 0.088	Eureka Valley
93.139.1413	37.13	-117.78	4.89 ± 0.024	5.37 ± 0.054	Eureka Valley
93.148.0447	35.18	-119.11	4.79 ± 0.000	5.02 ± 0.079	Bakersfield
93.223.2233	37.30	-121.69	4.87 ± 0.126	4.94 ± 0.089	San Felipe
93.262.2049	38.12	-122.45	3.47 ± 0.020	3.47 ± 0.073	Rogers Creek
93.262.2110	38.12	-122.44	3.58 ± 0.014	3.45 ± 0.101	Rogers Creek
93.266.0621	41.93	-122.03	4.60 ± 0.010	4.23 ± 0.053	Klamath Falls
93.284.0719	36.56	-121.22	4.27 ± 0.107	4.21 ± 0.038	Pinnacles
93.294.1437	36.15	-118.03	3.92 ± 0.055	4.29 ± 0.075	Owens Valley
93.318.1225	35.93	-120.52	4.83 ± 0.010	4.99 ± 0.063	Parkfield
93.338.2215	42.27	-122.03	5.41 ± 0.010	5.49 ± 0.032	Klamath Falls
94.011.1053	36.98	-121.72	4.12 ± 0.051	4.31 ± 0.051	Watsonville
94.017.1230	34.21	-118.54	6.71 ± 0.022	6.85 ± 0.054	Northridge
94.017.1756	34.22	-118.58	4.51 ± 0.070	4.62 ± 0.051	Northridge
94.017.2046	34.30	-118.58	5.01 ± 0.031	5.39 ± 0.035	Northridge
94.019.2111	34.38	-118.62	5.27 ± 0.014	5.59 ± 0.033	Northridge
94.032.0801	37.27	-118.36	3.93 ± 0.101	4.28 ± 0.059	Bishop
94.052.1340	40.43	-125.10	4.50 ± 0.049	4.21 ± 0.042	Mendocino
94.079.2120	34.28	-118.47	5.27 ± 0.075	5.34 ± 0.041	Northridge
94.096.1901	34.19	-117.10	4.53 ± 0.025	5.10 ± 0.022	San Bernardino
94.111.1637	36.30	-120.44	4.42 ± 0.009	4.55 ± 0.096	Coalinga
94.139.1643	36.57	-121.24	4.09 ± 0.054	3.21 ± 0.051	Pinnacles
94.139.1645	36.57	-121.24	4.09 ± 0.054	3.94 ± 0.053	Pinnacles
94.144.2011	40.92	-124.90	3.60 ± 0.043	3.69 ± 0.101	Mendocino
94.145.1256	34.31	-118.39	4.40 ± 0.030	4.72 ± 0.026	Northridge
94.170.1039	40.36	-124.58	4.93 ± 0.008	4.91 ± 0.054	Petrolia
94.177.0842	37.91	-122.32	4.17 ± 0.011	4.15 ± 0.074	Berkeley
94.183.1343	40.24	-124.47	3.94 ± 0.024	3.64 ± 0.058	Mendocino
94.184.2342	37.89	-118.26	3.62 ± 0.012	3.62 ± 0.026	Bishop
94.213.2134	34.63	-116.52	4.41 ± 0.053	4.87 ± 0.044	Landers
94.240.0122	36.81	-121.19	3.89 ± 0.079	4.06 ± 0.037	Tres Pinos
94.241.0509	38.81	-122.82	4.02 ± 0.090	3.26 ± 0.059	Geysers
94.244.1515	40.44	-125.90	6.93 ± 0.015	6.83 ± 0.037	Mendocino
94.250.1910	37.51	-121.26	4.01 ± 0.011	4.14 ± 0.080	Modesto
94.255.1223	38.83	-119.67	5.98 ± 0.093	6.15 ± 0.043	Double Spring Flat
94.255.2357	38.82	-119.66	5.20 ± 0.074	5.44 ± 0.039	Double Spring Flat
94.256.1149	38.76	-119.65	3.91 ± 0.057	4.21 ± 0.048	Double Spring Flat
94.256.2122	38.82	-119.66	4.18 ± 0.049	4.49 ± 0.046	Double Spring Flat
94.260.0259	38.74	-119.71	3.48 ± 0.055	4.05 ± 0.047	Double Spring Flat
94.260.1236	38.73	-119.71	3.79 ± 0.045	4.17 ± 0.048	Double Spring Flat
94.262.0725	38.75	-119.61	3.81 ± 0.023	4.07 ± 0.065	Double Spring Flat
94.262.1406	38.73	-119.74	3.67 ± 0.029	4.07 ± 0.058	Double Spring Flat
94.264.0209	40.44	-124.66	4.62 ± 0.000	4.70 ± 0.106	Mendocino FZ
94.270.1125	40.65	-124.06	3.84 ± 0.015	3.70 ± 0.074	Eureka
94.283.0307	38.75	-119.64	4.39 ± 0.039	4.86 ± 0.048	Double Spring Flat
94.284.2313	36.85	-121.61	3.73 ± 0.067	3.69 ± 0.088	San Juan Bautista
94.318.0128	40.36	-124.51	4.59 ± 0.007	4.38 ± 0.049	Mendocino

(continued)



## Appendix E (Continued)

Date/Time	Lat	Long	$M_w \pm \sigma$	$M_L \pm \sigma$	Location
94.321.2029	42.44	-122.18	4.37 ± 0.019	4.48 ± 0.055	Klamath
94.338.1035	37.35	-121.71	3.76 ± 0.089	3.69 ± 0.063	Alum Rock
94.341.0321	37.35	-121.71	4.02 ± 0.091	3.82 ± 0.068	Alum Rock
94.354.1027	35.89	-120.50	4.97 ± 0.004	5.08 ± 0.040	Parkfield
94.355.0550	38.74	-119.70	4.05 ± 0.057	4.31 ± 0.044	Double Spring Flat
94.360.1410	40.76	-124.37	5.47 ± 0.045	5.32 ± 0.043	Eureka
95.006.0012	38.78	-119.71	4.43 ± 0.045	4.72 ± 0.043	Double Spring Flat
95.008.0100	40.42	-127.39	4.73 ± 0.001	4.50 ± 0.051	Petrolia
95.032.2204	40.87	-121.24	3.65 ± 0.028	3.95 ± 0.071	Burney
95.050.0403	40.60	-126.03	6.61 ± 0.050	6.34 ± 0.044	Gorda Plate
95.059.2309	38.92	-122.63	4.25 ± 0.090	4.03 ± 0.039	Clear Lake
95.060.1055	40.68	-125.71	4.64 ± 0.026	4.34 ± 0.032	Offshore Petrolia
95.064.0007	37.60	-118.84	4.17 ± 0.008	4.59 ± 0.042	Mammoth
95.112.1431	38.76	-119.71	4.37 ± 0.117	4.58 ± 0.040	Markleeville
95.113.0841	36.58	-121.24	4.97 ± 0.071	5.03 ± 0.045	Pinnacles
95.122.1256	40.18	-123.19	4.04 ± 0.045	3.76 ± 0.106	Covelo
95.126.1246	40.40	-123.70	3.79 ± 0.043	3.61 ± 0.073	Petrolia
95.127.1103	33.90	-116.28	4.70 ± 0.040	5.04 ± 0.046	Indio
95.135.2157	40.44	-125.49	4.09 ± 0.005	4.18 ± 0.092	Mendocino FZ
95.137.0229	39.81	-122.70	4.57 ± 0.148	4.42 ± 0.060	Covelo
95.147.0549	38.80	-119.69	3.92 ± 0.026	4.10 ± 0.059	Markleeville
95.167.0420	36.75	-121.37	3.94 ± 0.033	3.98 ± 0.054	Hollister
95.169.2223	39.84	-120.72	4.11 ± 0.016	4.42 ± 0.044	Quincy
95.177.0840	34.30	-118.70	4.95 ± 0.010	5.28 ± 0.037	Castaic
95.193.2158	36.57	-121.23	4.01 ± 0.057	4.12 ± 0.045	San Benito

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